

# Model-Based Machine Learning for Physical-Layer Communication over Optical Fiber

Christian Häger

Department of Electrical Engineering, Chalmers University of Technology, Sweden

Summer School on “AI for Optical Networks &  
Neuromorphic Photonics for AI Acceleration”  
September 6, 2021



**CHALMERS**

## Thank You!



**Henry D. Pfister**  
Duke



**Christoffer Fougstedt**  
Chalmers (now: Ericsson)



**Lars Svensson**  
Chalmers



**Per Larsson-Edefors**  
Chalmers



**Rick M. Büttler**  
TU/e (now: TU Delft)



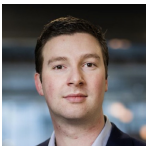
**Gabriele Liga**  
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**Alex Alvarado**  
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**Vinícius Oliari**  
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**Sebastiaan Goossens**  
TU/e



**Menno van den Hout**  
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**Sjoerd van der Heide**  
TU/e



**Chigo Okonkwo**  
TU/e

## Motivation and Challenges

### Global IP Traffic Growth

Global IP traffic will increase 3-fold from 2017 to 2022

26% CAGR  
2017-2022



Source: Cisco 2017

- The **COVID-19 pandemic** has highlighted the **importance** of our **global communication infrastructure**
- **Data traffic** has been and will continue to **grow exponentially**
- Simply **scaling current technology** is **not sustainable**: fiber infrastructure would consume all world-wide electricity within less than 10 years

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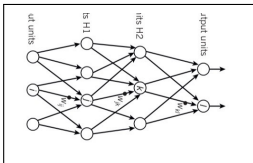
- Higher data rates?
- More energy efficiency?
- New functionalities?

- The **COVID-19 pandemic** has highlighted the **importance** of our **global communication infrastructure**
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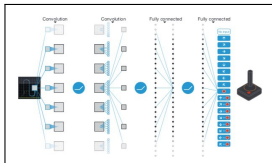
How can **machine learning (ML)** be used productively in communications to improve future systems?

This work started with a simple observation ...

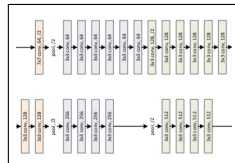
Deep Learning [LeCun et al., 2015]



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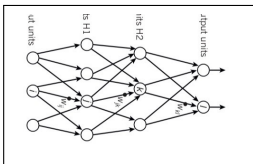


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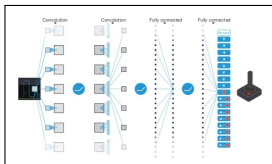
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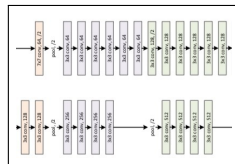
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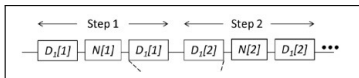


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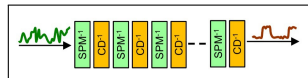


...

**Multi-layer neural networks:** impressive performance, countless applications



[Du and Lowery, 2010]



[Nakashima et al., 2017]

**Split-step methods** for solving the propagation equation in fiber-optics

# Agenda

In this talk, we ...

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1. show that **multi-layer neural networks** and the **split-step method** have the same functional form: both alternate **linear** and **pointwise nonlinear** steps



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2. propose a **physics-based machine-learning** approach based on **parameterizing** the split-step method (**no black-box** neural networks)

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2. propose a **physics-based machine-learning** approach based on **parameterizing** the split-step method (**no black-box** neural networks)
3. revisit **hardware-efficient** nonlinear equalization via **learned digital backpropagation**

# Outline

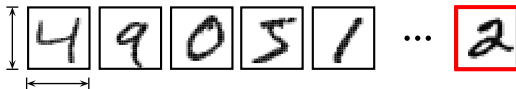
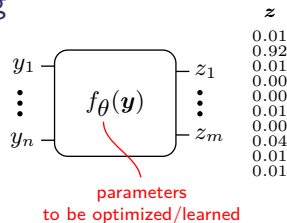
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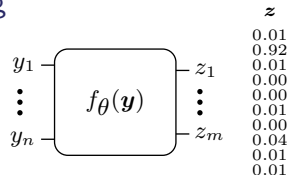
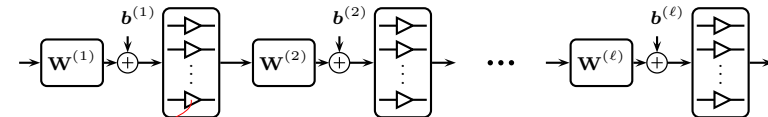
## Supervised Learning

handwritten digit recognition (MNIST: 70,000 images)

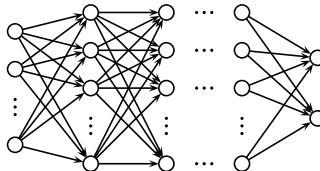
 $28 \times 28$  pixels $\Rightarrow n = 784$ 

## Supervised Learning

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How to choose  $f_{\theta}(y)$ ? **Deep feed-forward neural networks**

activation function



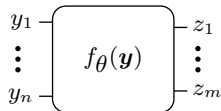
equivalent graph representation

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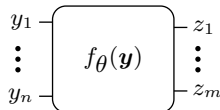
...


 $z$   
 0.01  
 0.92  
 0.01  
 0.00  
 0.00  
 0.01  
 0.00  
 0.00  
 0.04  
 0.01  
 0.01

How to optimize  $\theta = \{W^{(1)}, \dots, W^{(\ell)}, b^{(1)}, \dots, b^{(\ell)}\}$ ?

## Supervised Learning

handwritten digit recognition (MNIST: 70,000 images)



$z$	$x$
0.01	0
0.92	1
0.01	0
0.00	0
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How to optimize  $\theta = \{\mathbf{W}^{(1)}, \dots, \mathbf{W}^{(\ell)}, \mathbf{b}^{(1)}, \dots, \mathbf{b}^{(\ell)}\}$ ?

Given a **data set**  $\mathcal{D} = \{(\mathbf{y}^{(i)}, \mathbf{x}^{(i)})\}_{i=1}^N$ , where  $\mathbf{y}^{(i)}$  are **model inputs** and  $\mathbf{x}^{(i)}$  are **labels**, we iteratively minimize

$$\frac{1}{|\mathcal{B}_k|} \sum_{(\mathbf{y}, \mathbf{x}) \in \mathcal{B}_k} \mathcal{L}(f_{\theta}(\mathbf{y}), \mathbf{x}) \triangleq g(\theta) \quad \text{using} \quad \theta_{k+1} = \theta_k - \lambda \nabla_{\theta} g(\theta_k)$$

stochastic gradient descent

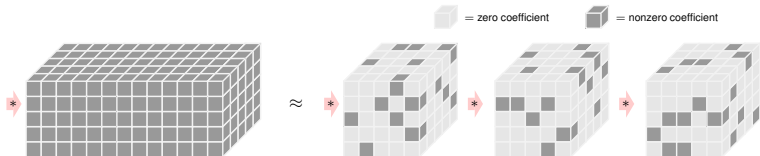
- $\mathcal{B}_k \subset \mathcal{D}$  and  $|\mathcal{B}_k|$  is called the **batch (or minibatch) size**
- Typical **loss function**: mean squared error  $\mathcal{L}(\mathbf{a}, \mathbf{b}) = \|\mathbf{a} - \mathbf{b}\|^2$  (regression)
- $\lambda$  is called the **step size** or **learning rate**



## Why Deep Models?

### Many possible answers

One advantage is complexity: **deep** computation graphs tend to be **more parameter efficient than shallow** graphs [Lin et al., 2017]



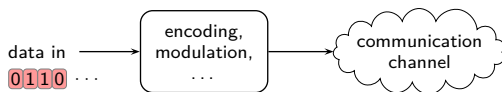
- **Sparsity** can emerge due to **(approximate) factorization** (even for linear models, e.g., FFT)
- Deep computation graphs allow for **very simple elementary steps**
- Deep models typically have **many “good” parameter configurations** that are close to each other  $\implies$  **robustness** to, e.g., quantization noise

# Physical-Layer Design: Conventional vs. Machine Learning



- **Conventional:** **handcrafted** DSP blocks based on **mathematical modeling**

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- Use function approximators and **learn** parameter configurations  $\theta$  **from data**

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[Shen and Lau, 2011], Fiber nonlinearity compensation using extreme learning machine for DSP-based ..., (*OECC*)  
 [Giacoumidis et al., 2015], Fiber nonlinearity-induced penalty reduction in CO-OFDM by ANN-based ..., (*Opt. Lett.*)

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# Physical-Layer Design: Conventional vs. Machine Learning



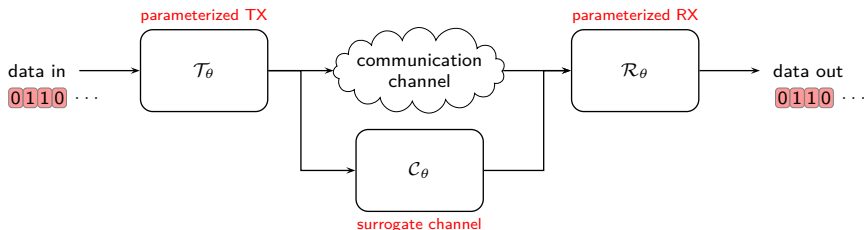
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- **Joint transmitter–receiver learning** via autoencoder [O’Shea and Hoydis, 2017]

[Karanov et al., 2018], End-to-end deep learning of optical fiber communications (*J. Lightw. Technol.*)

[Li et al., 2018], Achievable information rates for nonlinear fiber communication via end-to-end autoencoder learning, (*ECOC*)

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# Physical-Layer Design: Conventional vs. Machine Learning



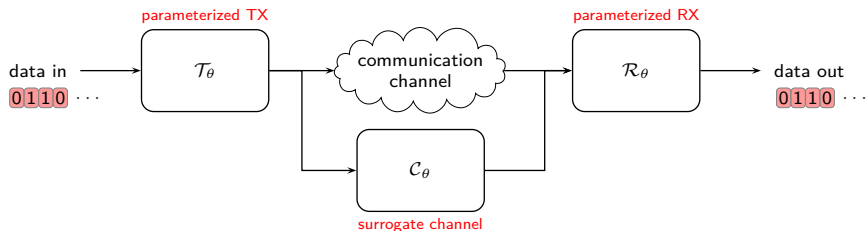
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- Use function approximators and learn parameter configurations  $\theta$  from data
- Joint transmitter–receiver learning via autoencoder [O’Shea and Hoydis, 2017]
- Surrogate channel models for gradient-based TX training

[O’Shea et al., 2018], Approximating the void: Learning stochastic channel models from observation with variational GANs, (arXiv)  
 [Ye et al., 2018], Channel agnostic end-to-end learning based communication systems with conditional GAN, (arXiv)

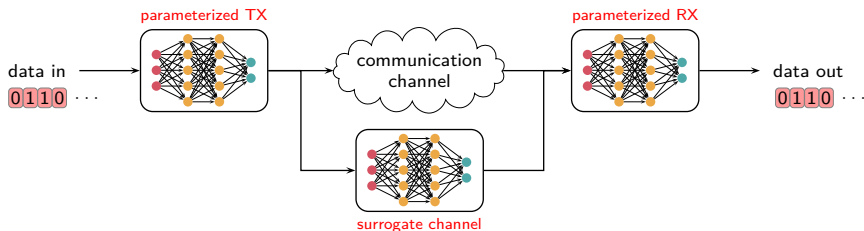
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# Physical-Layer Design: Conventional vs. Machine Learning



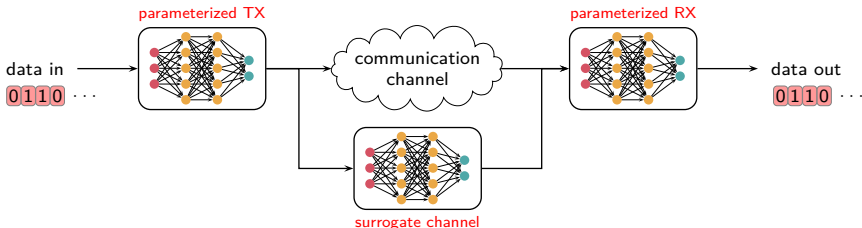
## Physical-Layer Design: Conventional vs. Machine Learning



Using (deep) neural networks for  $\mathcal{T}_\theta, \mathcal{R}_\theta, \mathcal{C}_\theta$ ? Possible, but ...

- How to **choose the network architecture** (#layers, activation function)?
- How to **limit the number of parameters** (complexity)?
- How to **interpret the solutions**? Any **insight** gained?
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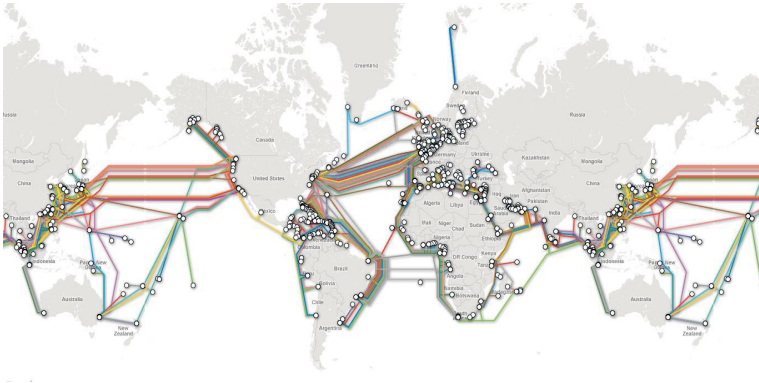
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**Our contribution:** designing “neural-network-like” machine-learning models by exploiting the underlying physics of the propagation.

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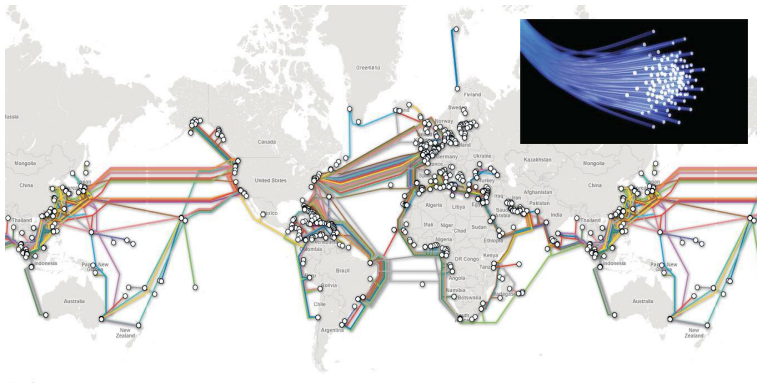
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## Fiber-Optic Communications



Fiber-optic systems enable **data traffic over very long distances** connecting cities, countries, and continents.

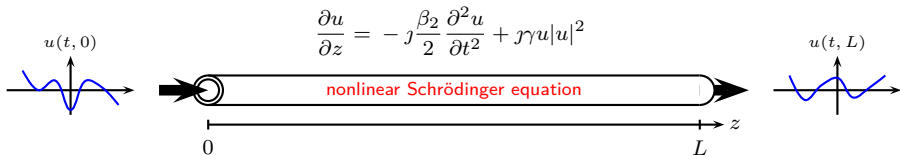
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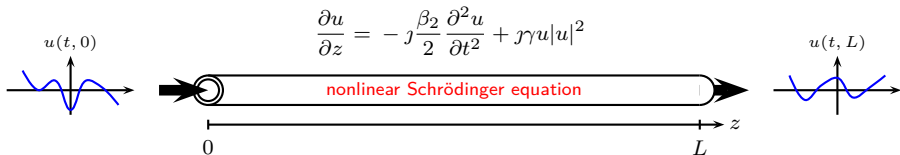
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- **Dispersion:** different wavelengths travel at different speeds (linear)
- **Kerr effect:** refractive index changes with signal intensity (nonlinear)

## Nonlinear Fiber Channel Modeling



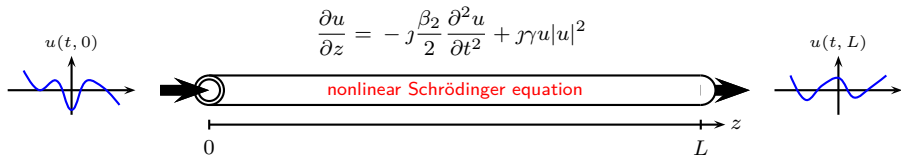
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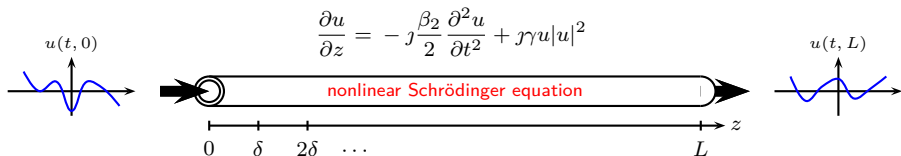


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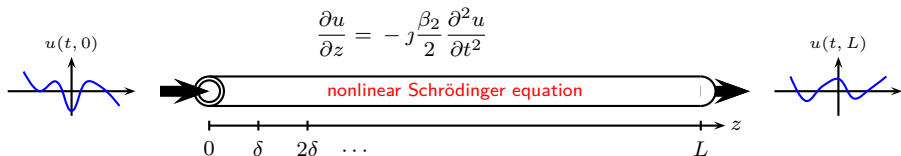
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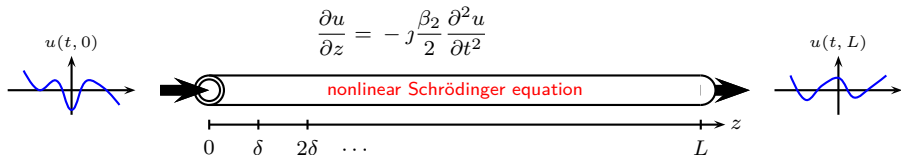
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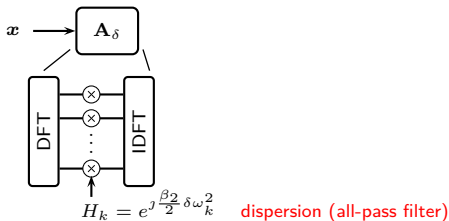


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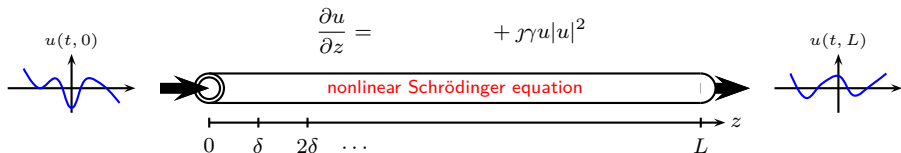
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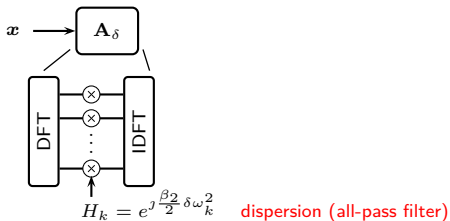
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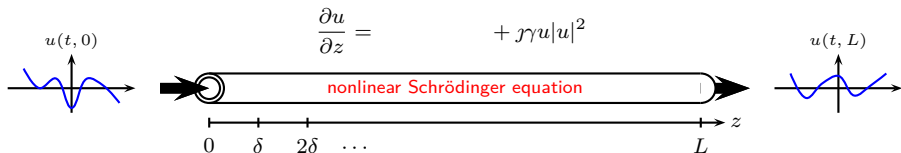
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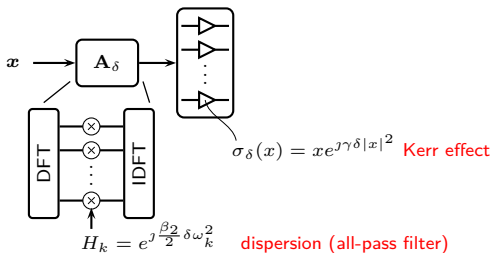
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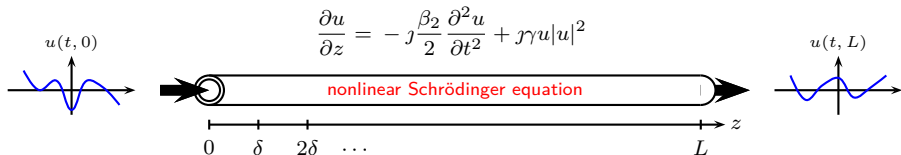
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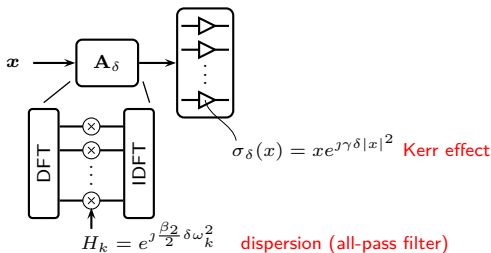
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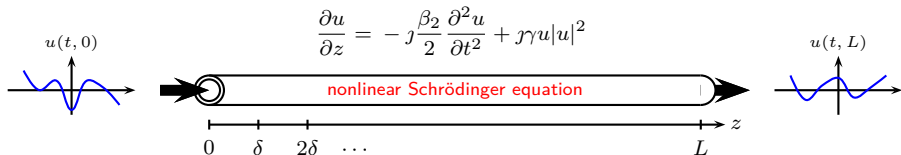
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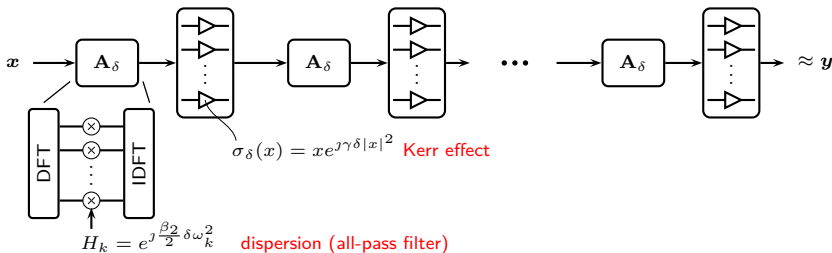
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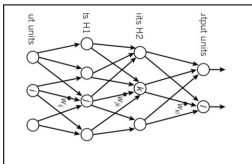


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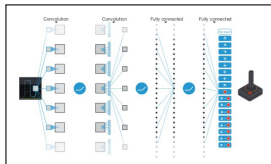




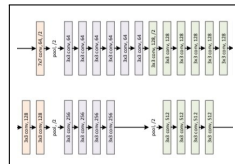
Deep Learning [LeCun et al., 2015]



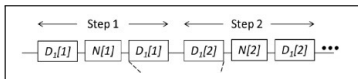
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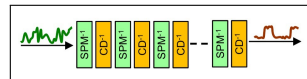
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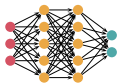


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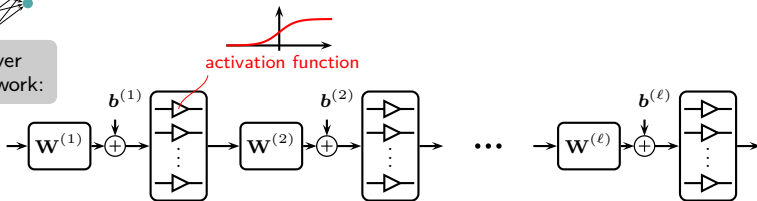


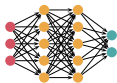
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## The Main Idea

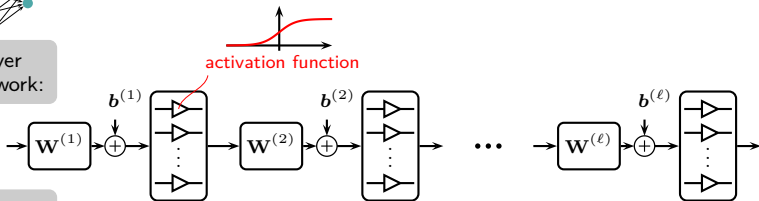


multi-layer  
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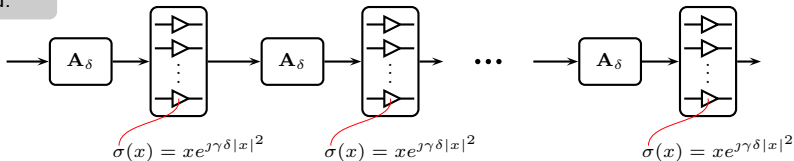




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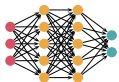


split-step  
method:

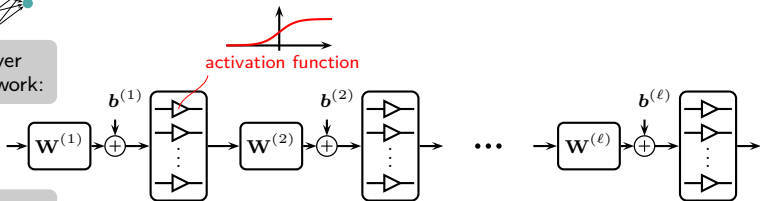


- This almost looks like a deep neural net!

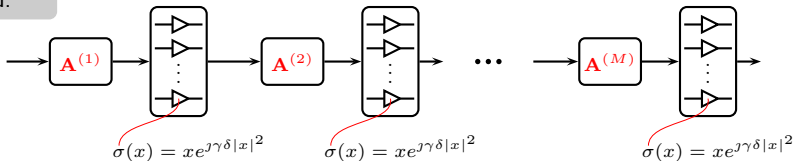
## The Main Idea



multi-layer  
neural network:



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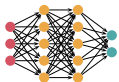


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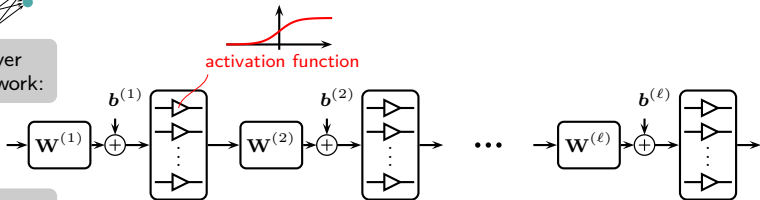
[Häger & Pfister, 2018], Nonlinear Interference Mitigation via Deep Neural Networks, (OFC)

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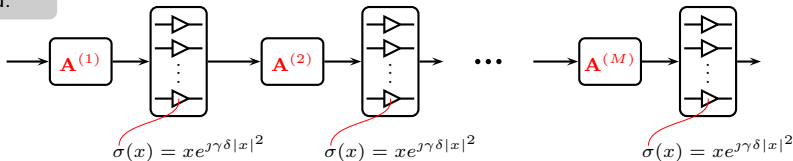
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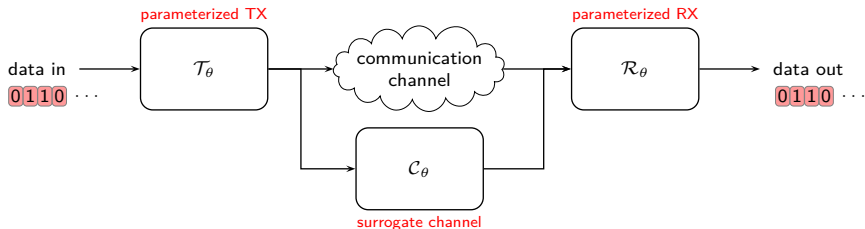


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- Special cases: step-size optimization, nonlinear operator “placement”, ...

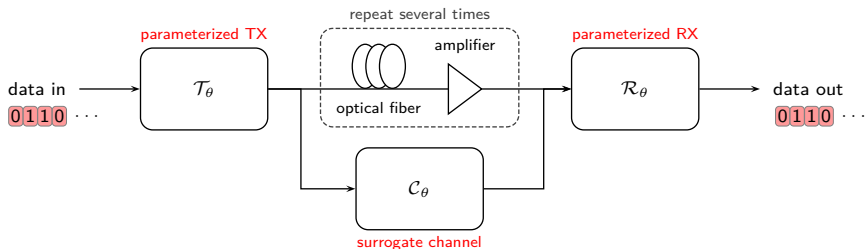
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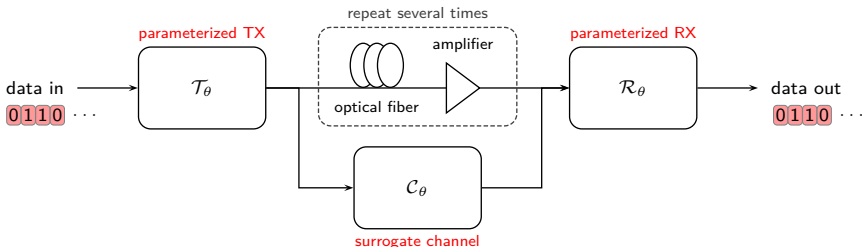
## Possible Applications



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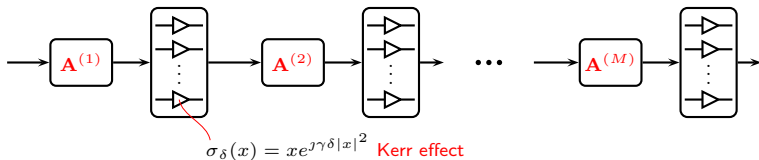
## Possible Applications



- **Channel  $\mathcal{C}_\theta$** : fine-tune model based on experimental data, reduce simulation time [Leibrich and Rosenkranz, 2003], [Li et al., 2005]
- **Receiver  $\mathcal{R}_\theta$** : nonlinear equalization (**focus in this talk**)
- **Transmitter  $\mathcal{T}_\theta$** : digital pre-distortion [Essiambre and Winzer, 2005], [Roberts et al., 2006], "split" nonlinearity compensation [Lavery et al., 2016]

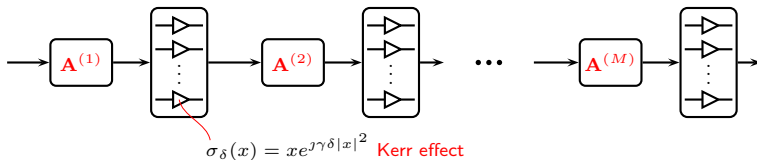


## Potential Benefits



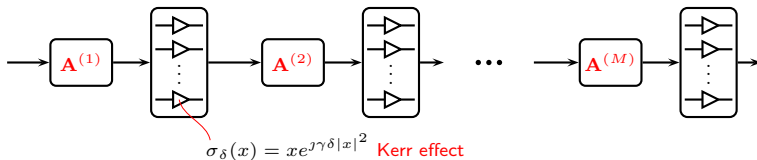
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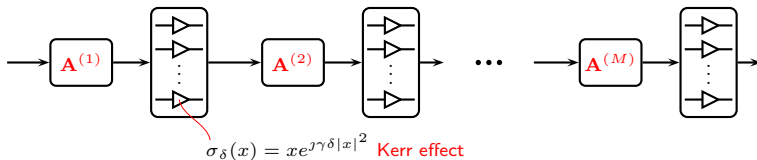
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  - Activation function is fixed; number of layers = number of steps
  - Hidden feature representations  $\approx$  signal at intermediate fiber locations
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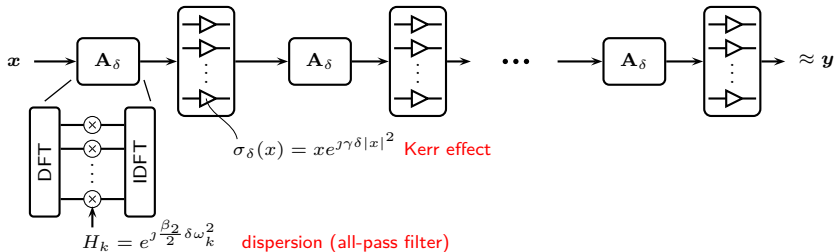


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  - Learned parameter configurations are interpretable
  - Satisfactory explanations for benefits over previous handcrafted solutions

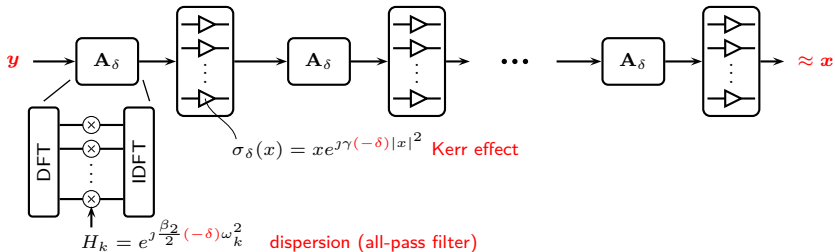
# Outline

1. Machine Learning and Neural Networks for Communications
2. Physics-Based Machine Learning for Fiber-Optic Communications
- 3. Learned Digital Backpropagation**
4. Polarization-Dependent Effects
5. Conclusions

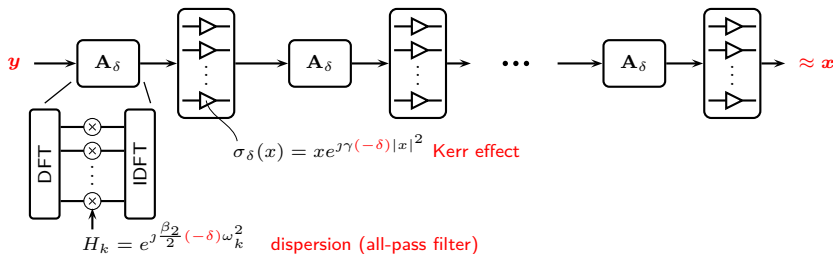
# Digital Backpropagation



## Digital Backpropagation



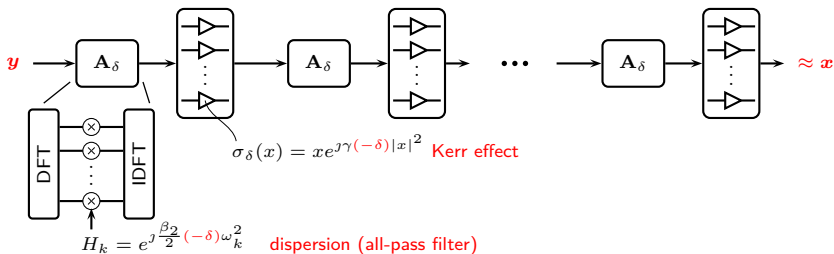
## Digital Backpropagation



- Fiber with negated parameters ( $\beta_2 \rightarrow -\beta_2$ ,  $\gamma \rightarrow -\gamma$ ) would perform perfect channel inversion [Paré et al., 1996] (ignoring attenuation)

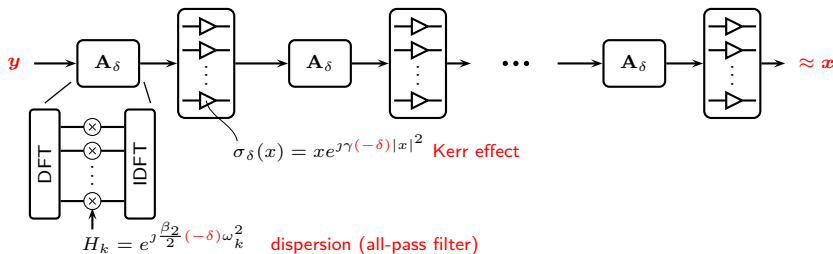


## Digital Backpropagation



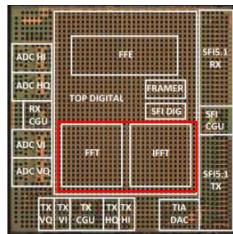
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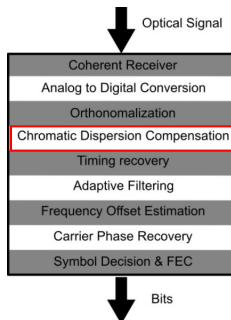


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- Widely considered to be impractical (**too complex**): linear equalization is already one of the **most power-hungry DSP blocks** in coherent receivers

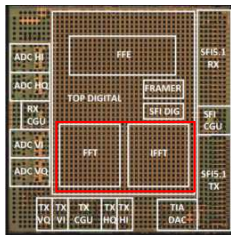
# Real-Time Digital Backpropagation



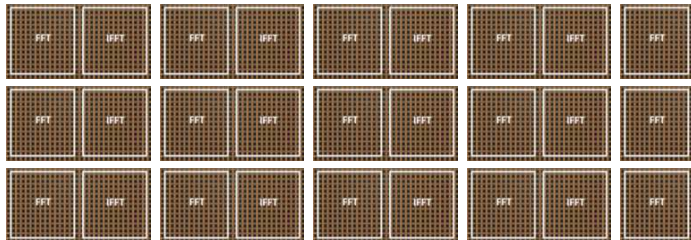
[Crivelli et al., 2014]



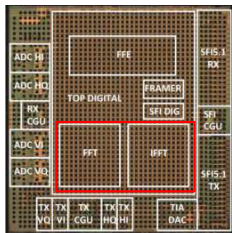
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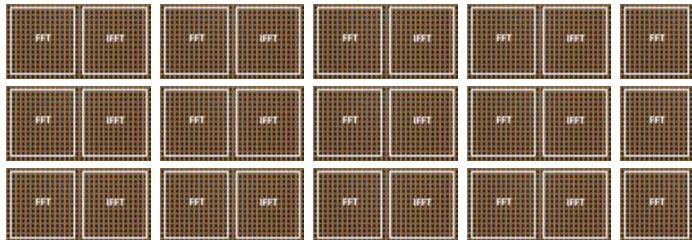
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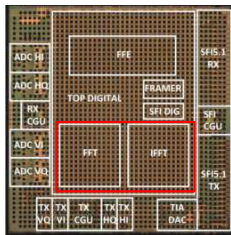


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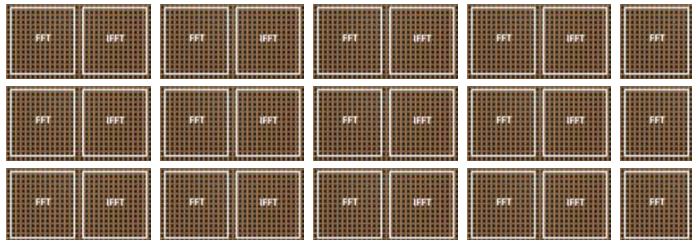


- Complexity increases with the number of steps  $M \implies$  **reduce  $M$  as much as possible** (see, e.g., [Du and Lowery, 2010], [Rafique et al., 2011], [Li et al., 2011], [Yan et al., 2011], [Napoli et al., 2014], [Secondini et al., 2016], . . .)

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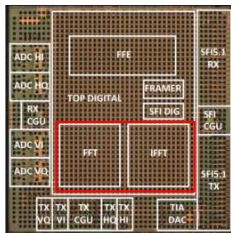


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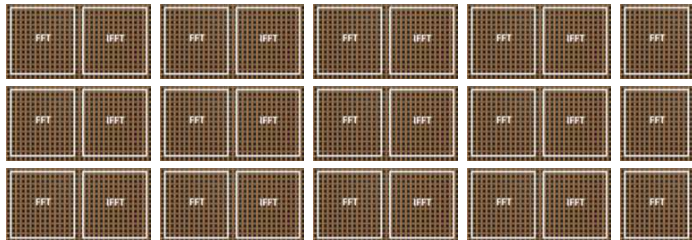


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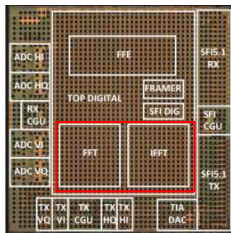


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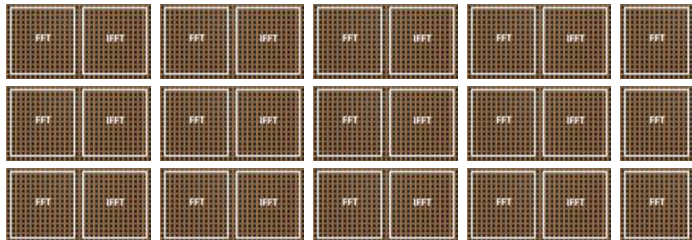


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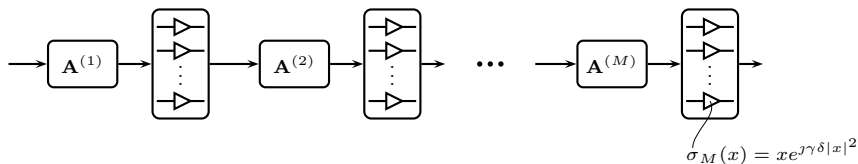
**Our approach: many steps but model compression**

**Joint optimization, pruning, and quantization of all linear steps  $\implies$  hardware-efficient digital backpropagation**



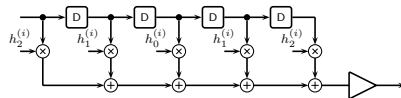
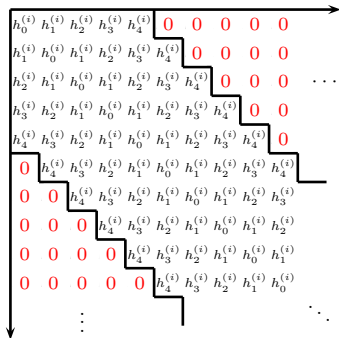
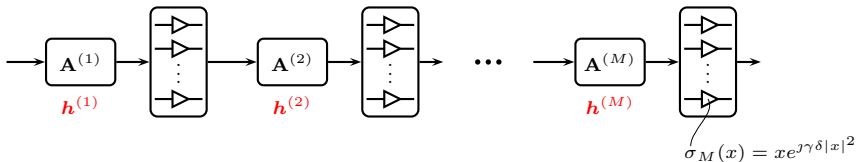
## Learned Digital Backpropagation

TensorFlow implementation of the computation graph  $f_{\theta}(\mathbf{y})$ :



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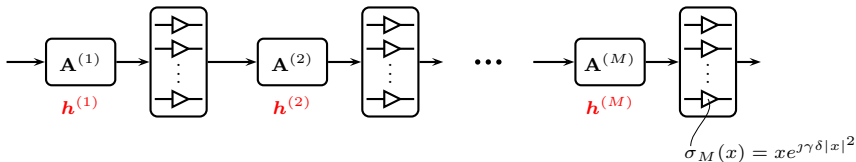
TensorFlow implementation of the computation graph  $f_{\theta}(\mathbf{y})$ :



finite impulse response (FIR) filter  
complex & symmetric coefficients

## Learned Digital Backpropagation

TensorFlow implementation of the computation graph  $f_{\theta}(\mathbf{y})$ :



Deep learning of all FIR filter coefficients  $\theta = \{\mathbf{h}^{(1)}, \dots, \mathbf{h}^{(M)}\}$ :

$$\min_{\theta} \sum_{i=1}^N \text{Loss}(f_{\theta}(\mathbf{y}^{(i)}), \mathbf{x}^{(i)}) \triangleq g(\theta)$$

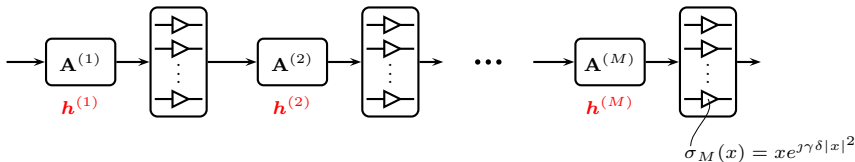
mean squared error

using  $\theta_{k+1} = \theta_k - \lambda \nabla_{\theta} g(\theta_k)$

Adam optimizer, fixed learning rate

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mean squared error
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Iteratively **prune (set to 0) outermost filter taps** during gradient descent

# Iterative Filter Tap Pruning

$$\theta = \left\{ \begin{array}{l} \mathbf{h}^{(1)} \\ \mathbf{h}^{(2)} \\ \vdots \\ \mathbf{h}^{(M)} \end{array} \right.$$

## Iterative Filter Tap Pruning

← starting length  $2K' + 1$  →

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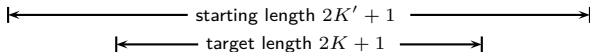
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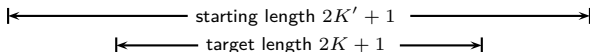


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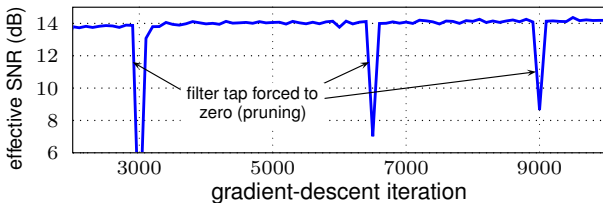
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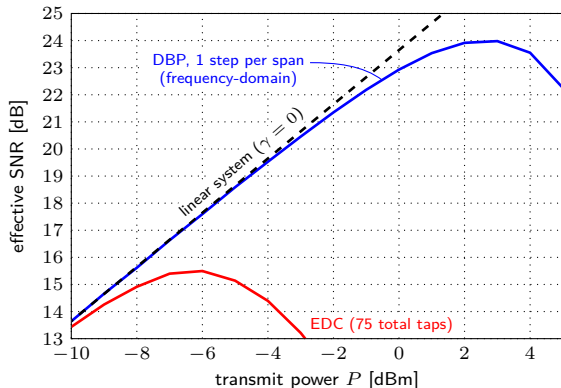
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- Typical **learning curve**:



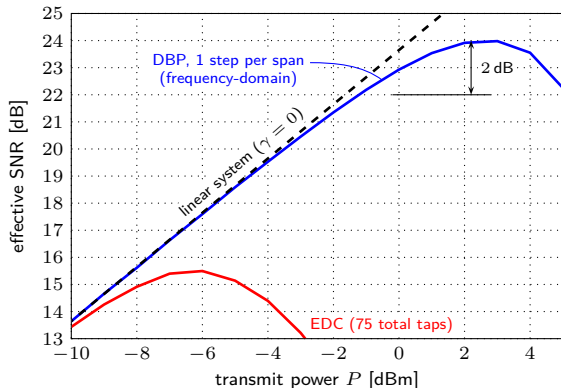
## Revisiting Ip and Kahn (2008)



Parameters similar to [Ip and Kahn, 2008]:

- 25 × 80 km SSFM
- Gaussian modulation
- RRC pulses (0.1 roll-off)
- 10.7 Gbaud
- 2 samples/symbol processing
- single channel, single pol.

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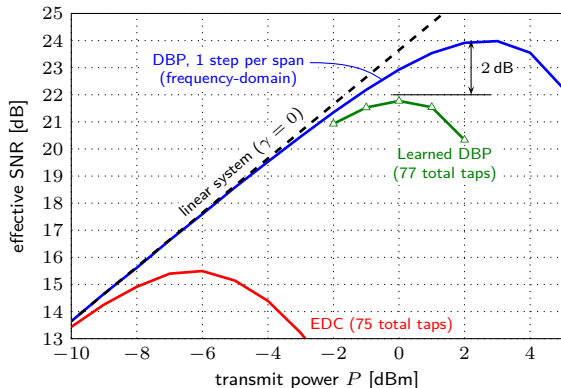


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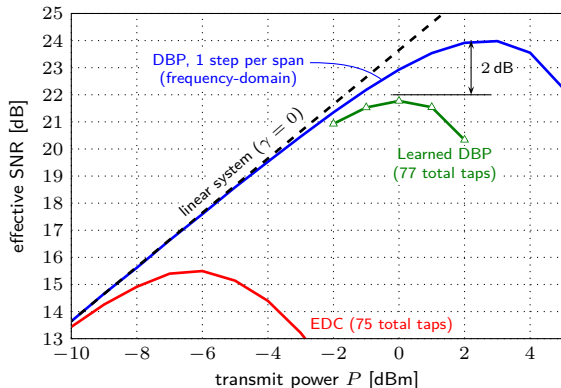


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- Learned approach uses **only 77 total taps**: alternate 5 and 3 taps/step and use **different** filter coefficients in all steps [Häger and Pfister, 2018a]

## Revisiting Ip and Kahn (2008)

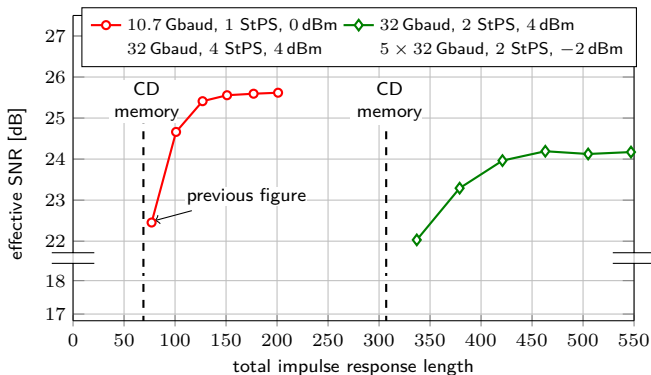


Parameters similar to [Ip and Kahn, 2008]:

- $25 \times 80$  km SSFM
- Gaussian modulation
- RRC pulses (0.1 roll-off)
- 10.7 Gbaud
- 2 samples/symbol processing
- single channel, single pol.

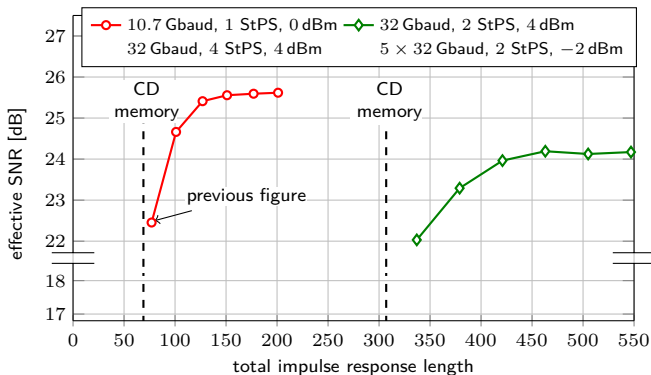
- $\gg 1000$  total taps (70 taps/step)  $\implies > 100\times$  complexity of EDC
- Learned approach uses **only 77 total taps**: alternate 5 and 3 taps/step and use **different** filter coefficients in all steps [Häger and Pfister, 2018a]
- Can **outperform "ideal DBP"** in the nonlinear regime [Häger and Pfister, 2018b]

## Performance–Complexity Trade-off





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**Conventional wisdom:** Steps are **inefficient**  $\implies$  reduce as much as possible

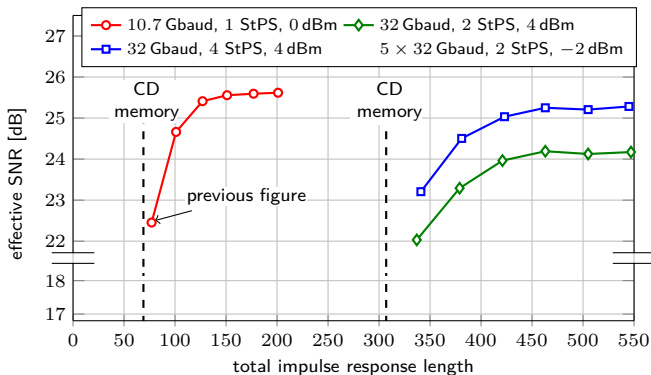
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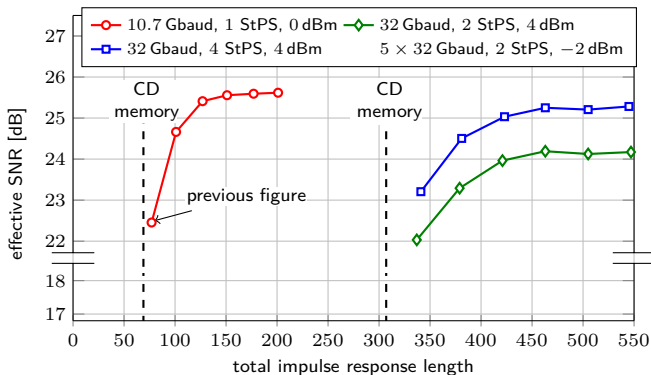
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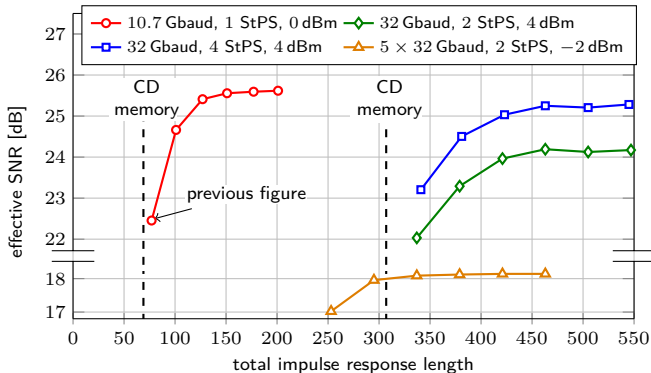
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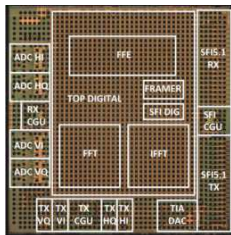
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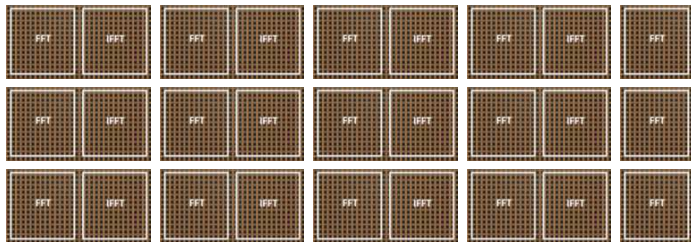
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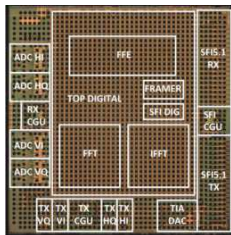
## Real-Time ASIC Implementation



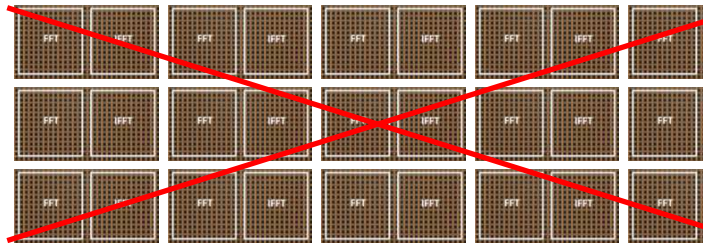
[Crivelli et al., 2014]



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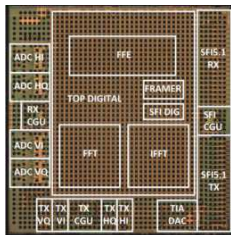


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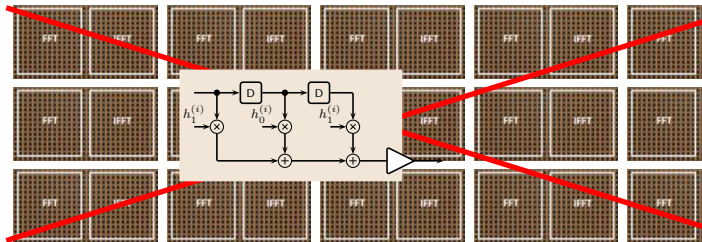


- [Fougstedt et al., 2017], Time-domain digital back propagation: Algorithm and finite-precision implementation aspects, (*OFC*)  
 [Fougstedt et al., 2018], ASIC implementation of time-domain digital back propagation for coherent receivers, (*PTL*)  
 [Sherborne et al., 2018], On the impact of fixed point hardware for optical fiber nonlinearity compensation algorithms, (*JLT*)

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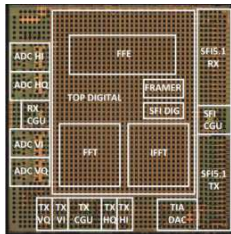


[Crivelli et al., 2014]

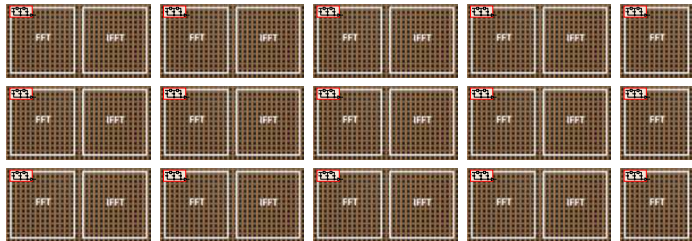


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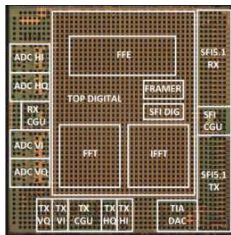


- Our linear steps are **very short symmetric FIR filters** (as few as **3 taps**)
- 28-nm ASIC at 416.7 MHz clock speed (40 GHz signal)
  - **Only 5-6 bit** filter coefficients via **learned quantization**
  - Hardware-friendly nonlinear steps (Taylor expansion)
  - All FIR filters are **fully reconfigurable**

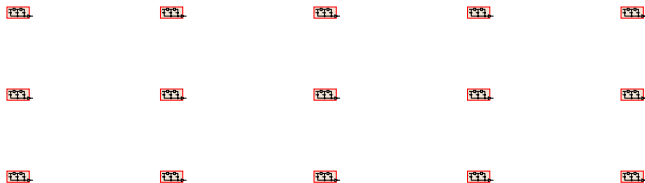
[Fougstedt et al., 2018], ASIC implementation of time-domain digital backpropagation with deep-learned chromatic dispersion filters, (ECOC)



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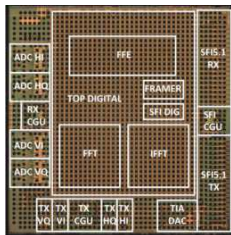
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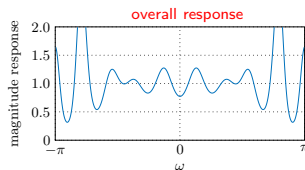
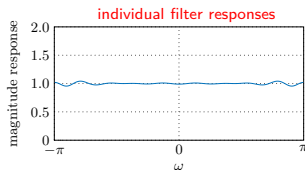
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  - **Only 5-6 bit filter coefficients via learned quantization**
  - **Hardware-friendly nonlinear steps (Taylor expansion)**
  - **All FIR filters are fully reconfigurable**
- **< 2× power compared to EDC** [Crivelli et al., 2014, Pillai et al., 2014]

[Fougstedt et al., 2018], ASIC implementation of time-domain digital backpropagation with deep-learned chromatic dispersion filters, (ECOC)

## Why Does The Learning Approach Work?

Previous work: design a single filter or filter pair and use it repeatedly.

⇒ Good overall response only possible with very long filters.



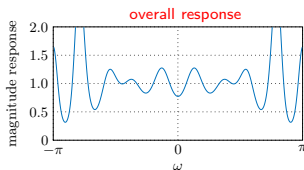
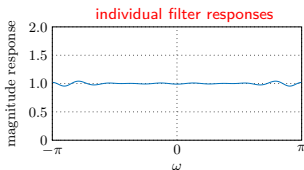
From [Ip and Kahn, 2009]:

- “We also note that [ . . . ] 70 taps, is much larger than expected”
- “This is due to amplitude ringing in the frequency domain”
- “Since backpropagation requires multiple iterations of the linear filter, amplitude distortion due to ringing accumulates (Goldfarb & Li, 2009)”

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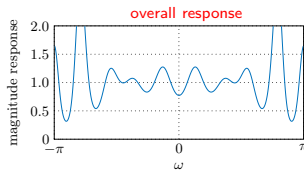
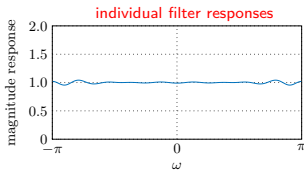
**The learning approach uncovered that there is no such requirement!**

[Lian, Häger, Pfister, 2018], What can machine learning teach us about communications? (*ITW*)

## Why Does The Learning Approach Work?

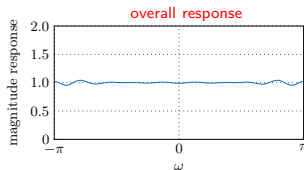
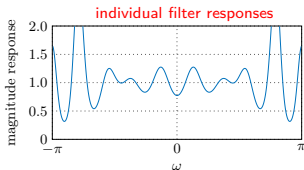
Previous work: design a single filter or filter pair and use it repeatedly.

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Sacrifice individual filter accuracy, but different response per step.

⇒ Good overall response even with very short filters by joint optimization.



## Experimental Investigations

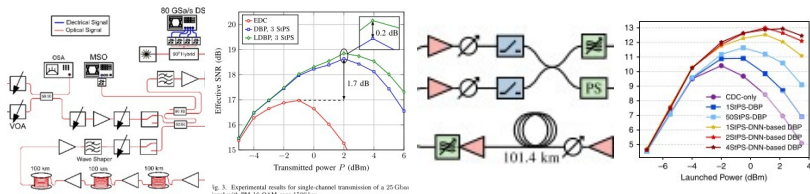


Fig. 3. Experimental results for single-channel transmission of a 25 Gba/s

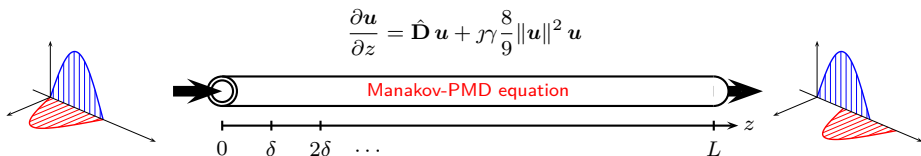
Training with **real-world data sets** including presence of various **hardware impairments** (phase noise, timing error, frequency offset, etc.)

- [Oliari et al., 2020], Revisiting Efficient Multi-step Nonlinearity Compensation with Machine Learning: An Experimental Demonstration, (*J. Lightw. Technol.*)
- [Sillekens et al., 2020], Experimental Demonstration of Learned Time-domain Digital Back-propagation, (*Proc. IEEE Workshop on Signal Processing Systems*)
- [Fan et al., 2020], Advancing Theoretical Understanding and Practical Performance of Signal Processing for Nonlinear Optical Communications through Machine Learning, (*Nat. Commun.*)
- [Bitachon et al., 2020], Deep learning based Digital Back Propagation Demonstrating SNR gain at Low Complexity in a 1200 km Transmission Link, (*Opt. Express*)

# Outline

1. Machine Learning and Neural Networks for Communications
2. Physics-Based Machine Learning for Fiber-Optic Communications
3. Learned Digital Backpropagation
4. Polarization-Dependent Effects
5. Conclusions

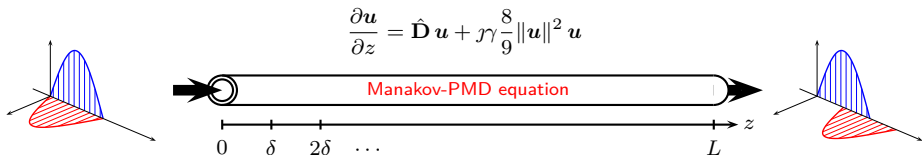
## Evolution of Polarization-Multiplexed Signals



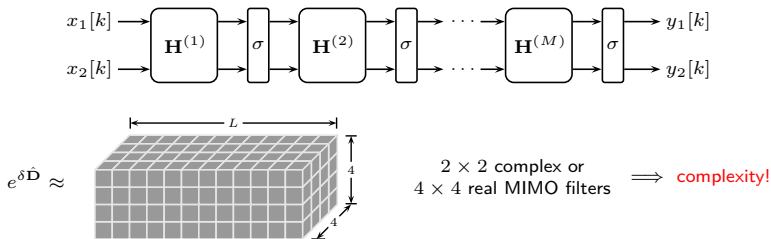
- Jones vector  $\mathbf{u} \triangleq (u_1(t, z), u_2(t, z))^T$  with complex baseband signals
- linear operator  $\hat{\mathbf{D}}$ : attenuation, chromatic & polarization mode dispersion



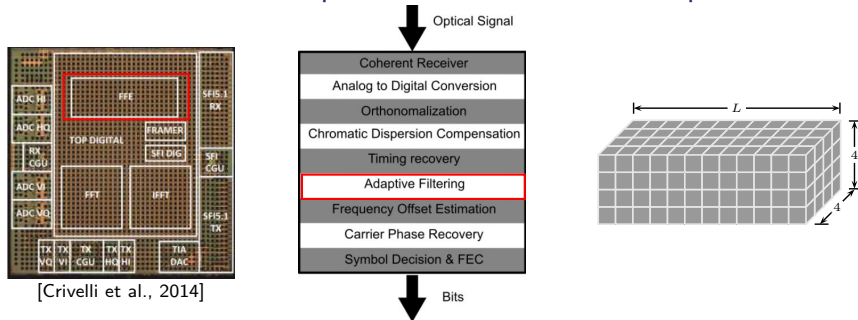
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- **linear operator  $\hat{\mathbf{D}}$** : attenuation, chromatic & polarization mode dispersion
- Split-step method: **alternate linear and nonlinear steps**  $\sigma(\mathbf{x}) = \mathbf{x} e^{\gamma \gamma \frac{8}{9} \delta \|\mathbf{x}\|^2}$

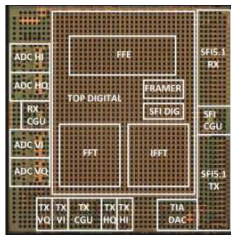


# Real-Time Compensation of Polarization Impairments

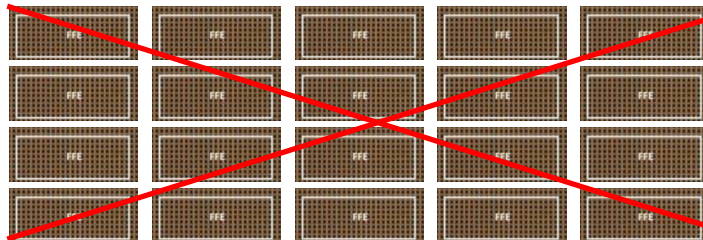


- **time-varying** effects (e.g., drifts) & a priori **unknown realizations**
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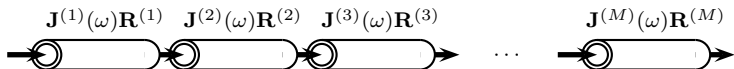


[Crivelli et al., 2014]



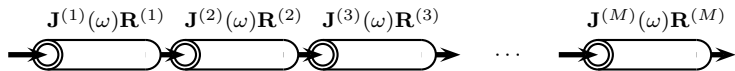
- **time-varying** effects (e.g., drifts) & a priori **unknown realizations**
  - $\implies$  **adaptive filtering** (via stochastic gradient descent) required
- Using (and updating) **full MIMO filters** in each step is **not feasible**.
  - We propose a **hardware-efficient machine-learning model** based on the propagation characteristics

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The overall PMD is modeled via  $M$  sections, where each section introduces

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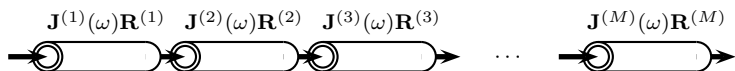


The overall PMD is modeled via  $M$  sections, where each section introduces

1. a **differential group delay (DGD)**  $\tau^{(k)}$ , described by

$$\mathbf{J}^{(k)}(\omega) = \begin{pmatrix} \exp\left(-j\omega\frac{\tau^{(k)}}{2}\right) & 0 \\ 0 & \exp\left(j\omega\frac{\tau^{(k)}}{2}\right) \end{pmatrix}$$

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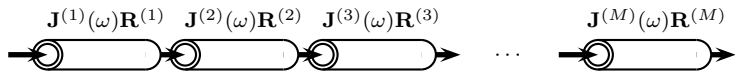
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2. a **rotation of the polarization state**, described by  $\mathbf{R}^{(k)} \in \text{SU}(2)$ , where

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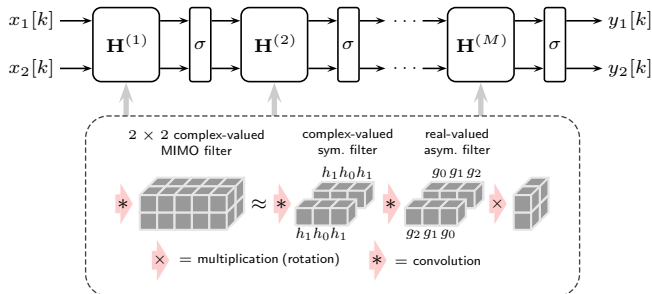
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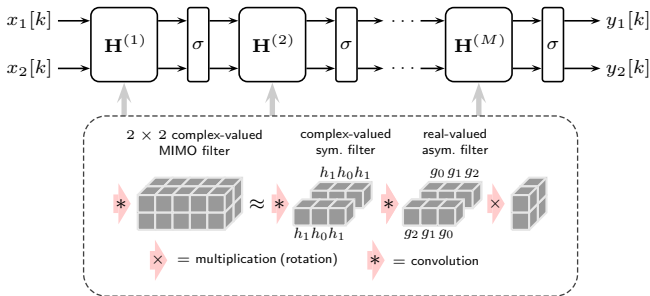
- (i) We **integrate** these operations in each step/layer
- (ii) We use real-valued (asymmetric) FIR filters to approximate DGD

## The Final Machine-Learning Model





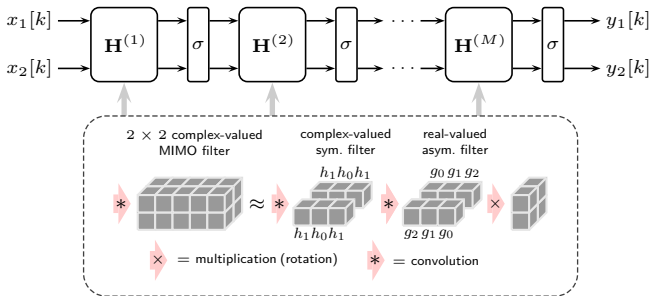
## The Final Machine-Learning Model



Each linear step consists of 3 trainable components

1. complex-valued (symmetric) filters that mainly account for dispersion
2. real-valued (asymmetric) filters for DGD
3. memoryless “rotation” matrices  $\begin{pmatrix} a & -b^* \\ b & a^* \end{pmatrix}$ , where  $a, b \in \mathbb{C}$  (4 real parameters)

## The Final Machine-Learning Model



Compared to prior work, our learning-based approach ...

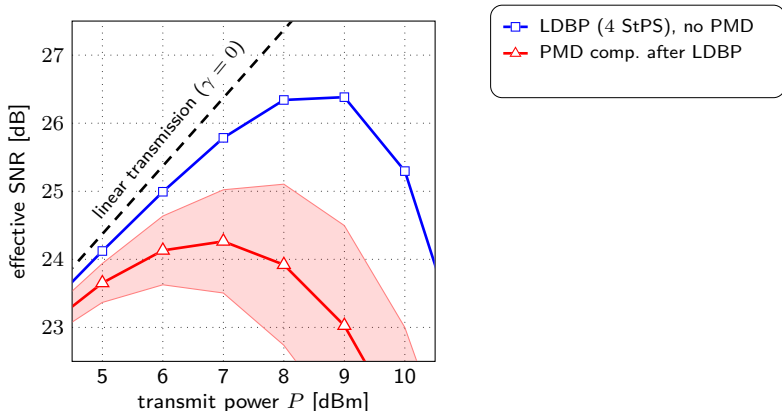
- **assumes no knowledge** about PMD realizations or **accumulated PMD**
- is FIR-filter based! **Avoids frequency-domain** (FFT-based) filtering

[Goroshko et al., 2016], Overcoming performance limitations of digital back propagation due to polarization mode dispersion, (*CTON*)

[Czegledi et al., 2017], Digital backpropagation accounting for polarization-mode dispersion, (*Opt. Express*)

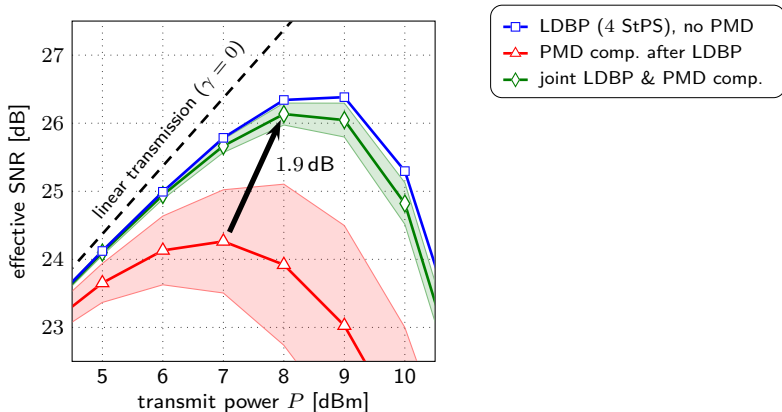
[Liga et al., 2018], A PMD-adaptive DBP receiver based on SNR optimization, (*OFIC*)

## Results (32 Gbaud, $10 \times 100$ km, $0.2 \text{ ps}/\sqrt{\text{km}}$ PMD)



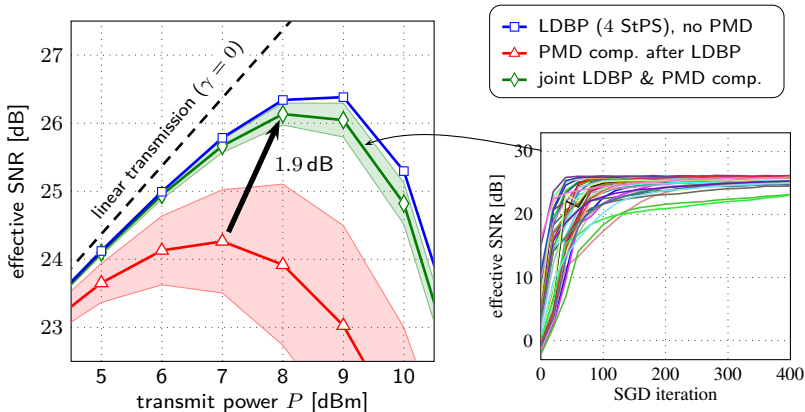
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- **Reliable convergence** “from scratch” + only 9 real parameters per step

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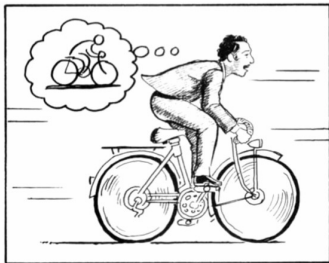
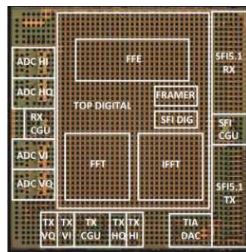


Figure 1. A World Model, from Scott McCloud's *Understanding Comics*. (McCloud, 1993; E, 2012)



[Crivelli et al., 2014]

- Optical receivers build models of their "environment"

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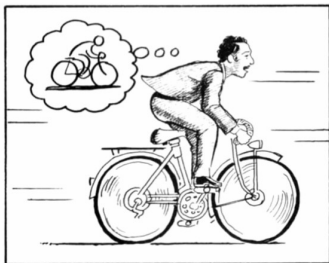
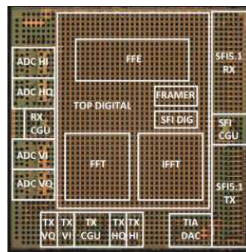


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[Crivelli et al., 2014]

- Optical receivers build models of their "environment"
- Currently these models are **linear** and/or **rigid** (non-adaptive)
- Interpretable **physics-based "multi-layer" models** for machine learning can be obtained by exploiting our existing domain knowledge



# Conclusions

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## Conclusions

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universal function approximators

good designs require  
experience and fine-tuning

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# Thank you!



# References I



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*In Proc. IEEE Int. Symp. Information Theory (ISIT)*, Vail, CO.



Häger, C. and Pfister, H. D. (2018b).  
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