Model-Based Machine Learning for Joint Digital Backpropagation and PMD Compensation

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> Optical Fiber Communications Conference (OFC) San Diego, USA, March 11, 2020

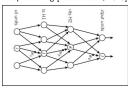








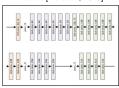




Deep Q-Learning [Mnih et al., 2015]

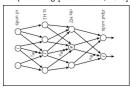


ResNet [He et al., 2015]



Multi-layer neural networks: impressive performance, countless applications

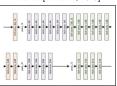




Deep Q-Learning [Mnih et al., 2015]



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Multi-layer neural networks: impressive performance, countless applications



[Nakashima et al., 2017]

Split-step methods for solving the propagation equation in fiber-optics

In this talk, we ...

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1. show that multi-layer neural networks and the split-step method have the same functional form: both alternate linear and pointwise nonlinear steps

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- propose a model-based machine-learning approach based on parameterizing the split-step method (no black-box neural networks)

In this talk, we ...

- 1. show that multi-layer neural networks and the split-step method have the same functional form: both alternate linear and pointwise nonlinear steps
- propose a model-based machine-learning approach based on parameterizing the split-step method (no black-box neural networks)
- 3. revisit hardware-efficient digital backpropagation combined with distributed compensation of polarization mode dispersion

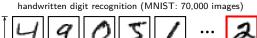
Outline

- 1. Machine Learning and Neural Networks for Communications
- 2. Model-Based Machine Learning for Fiber-Optic Communications
- 3. Learned Digital Backpropagation
- 4. Polarization-Dependent Effects
- 5. Conclusions

Outline

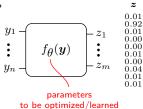
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Supervised Learning



 28×28 pixels $\implies n = 784$

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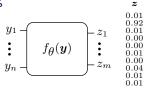
Supervised Learning

handwritten digit recognition (MNIST: 70,000 images)

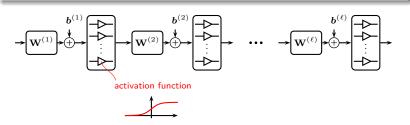


Machine Learning





How to choose $f_{\theta}(y)$? Deep feed-forward neural networks



Supervised Learning

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Machine Learning

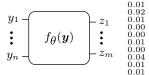




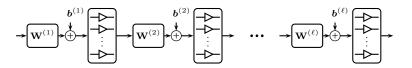








How to choose $f_{\theta}(y)$? Deep feed-forward neural networks



How to optimize $\theta = \{ \boldsymbol{W}^{(1)}, \dots, \boldsymbol{W}^{(\ell)}, \boldsymbol{b}^{(1)}, \dots, \boldsymbol{b}^{(\ell)} \}$? Deep learning

$$\min_{\theta} \sum_{i=1}^{N} \mathsf{Loss}(f_{\theta}(\boldsymbol{y}^{(i)}), \boldsymbol{x}^{(i)}) \triangleq g(\theta)$$
mean squared error
cross-entropy, ...

using
$$\theta_{k+1} = \theta_k - \lambda \nabla_{\theta} g(\theta_k)$$
 (1) stochastic gradient descent, RMSProp. Adam. . . .



Machine Learning



[Shen and Lau, 2011], Fiber nonlinearity compensation using extreme learning machine for DSP-based ..., (OECC) [Giacoumidis et al., 2015], Fiber nonlinearity-induced penalty reduction in CO-OFDM by ANN-based ..., (Opt. Lett.) [Zibar et al., 2016], Machine learning techniques in optical communication, (J. Lightw. Technol.) [Kamalov et al., 2018]. Evolution from 8gam live traffic to ps 64-gam with neural-network based nonlinearity compensation (OFC)



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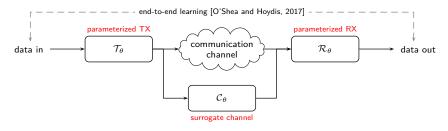
[O'Shea and Hoydis, 2017], An introduction to deep learning for the physical layer, (*IEEE Trans. Cogn. Commun. Netw.*) [Karanov et al., 2018], End-to-end deep learning of optical fiber communications (*J. Lightw. Technol.*)

[Jones et al., 2018], Deep learning of geometric constellation shaping including fiber nonlinearities, (ECOC)

[Li et al., 2018], Achievable information rates for nonlinear fiber communication via end-to-end autoencoder learning, (ECOC)

Machine Learning

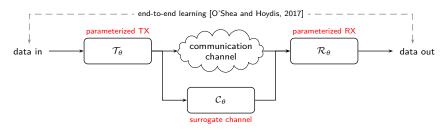
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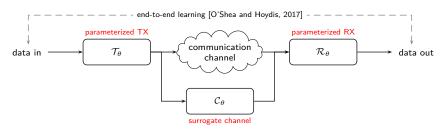
[O'Shea et al., 2018], Approximating the void: Learning stochastic channel models from observation with variational GANs, (arXiv) [Ye et al., 2018], Channel agnostic end-to-end learning based communication systems with conditional GAN, (arXiv)



Using neural networks for \mathcal{T}_{θ} , \mathcal{R}_{θ} , \mathcal{C}_{θ}

- How to choose network architecture (#layers, activation function)?
- How to initialize parameters?
- How to interpret solutions? Any insight gained?

Machine Learning



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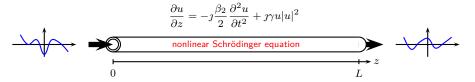
Machine Learning

Model-based learning: sparse signal recovery [Gregor and Lecun, 2010], [Borgerding and Schniter, 2016], neural belief propagation [Nachmani et al., 2016], radio transformer networks [O'Shea and Hoydis, 2017], ...

Outline

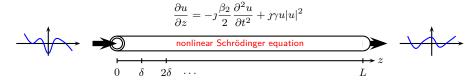
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The Split-Step Method

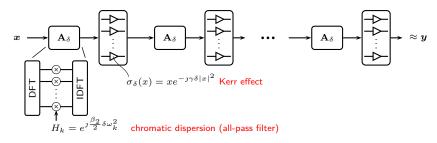


• Deterministic channel model: partial differential equation

The Split-Step Method

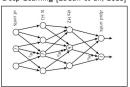


- Deterministic channel model: partial differential equation
- Split-step method with M steps ($\delta = L/M$):

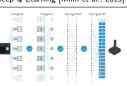


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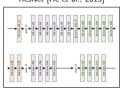




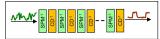
Deep Q-Learning [Mnih et al., 2015]



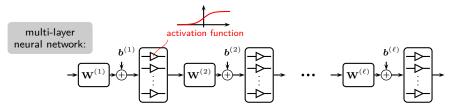
ResNet [He et al., 2015]

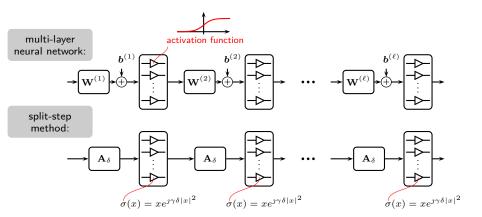


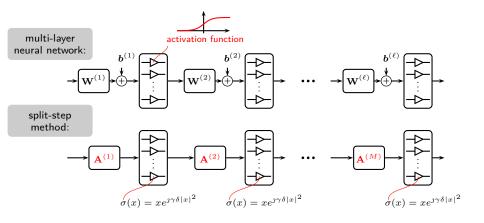
[Du and Lowery, 2010]



[Nakashima et al., 2017]

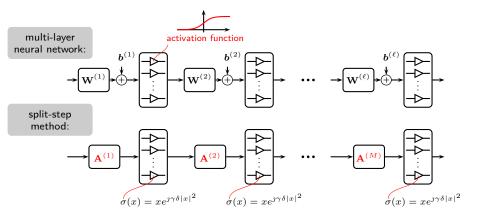




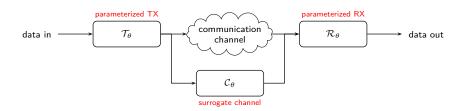


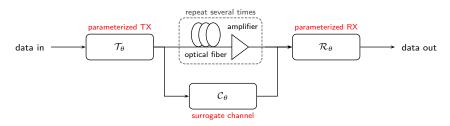
[[]Häger & Pfister, 2018], Nonlinear Interference Mitigation via Deep Neural Networks, (OFC)

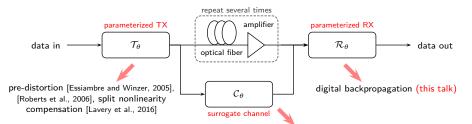
[[]Häger & Pfister, 2018], Deep Learning of the Nonlinear Schrödinger Equation in Fiber-Optic Communications, (ISIT)



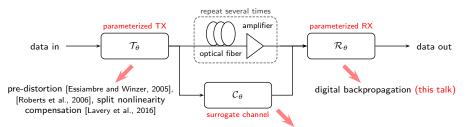
• Parameterized model f_{θ} with $\theta = \{\mathbf{A}^{(1)}, \dots, \mathbf{A}^{(M)}\}$







fine-tune with experimental data, reduce simulation time [Leibrich and Rosenkranz, 2003], [Li et al., 2005]



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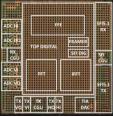
Model-based learning approaches

- How to choose network architecture (#layers, activation function)? √
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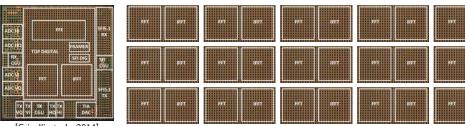
Real-Time Digital Backpropagation



[Crivelli et al., 2014]

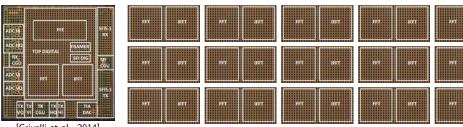
• Invert a partial differential equation in real time ([Paré et al., 1996], [Essiambre and Winzer, 2005], [Roberts et al., 2006], [Li et al., 2008], [Ip and Kahn, 2008])

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 - Widely considered to be impractical (too complex): linear equalization is already one of the most power-hungry DSP blocks in coherent receivers

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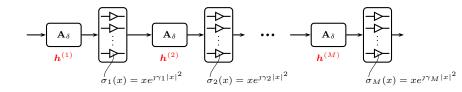
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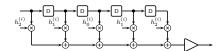
Our approach

Joint optimization, pruning, and quantization of all chromatic-dispersion filters leads to efficient digital backpropagation, even with many steps.

Learned Digital Backpropagation

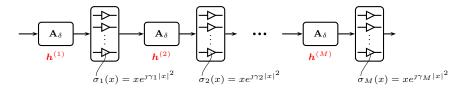
TensorFlow implementation of the computation graph $f_{\theta}(y)$:





Learned Digital Backpropagation

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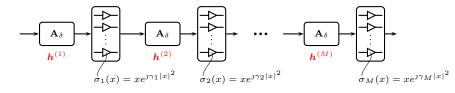
Deep learning of parameters $\theta = \{h^{(1)}, \dots, h^{(M)}\}$:

$$\min_{\theta} \sum_{i=1}^{N} \mathsf{Loss}(f_{\theta}(\boldsymbol{y}^{(i)}), \boldsymbol{x}^{(i)}) \triangleq g(\theta) \qquad \text{using} \quad \theta_{k+1} = \theta_{k} - \lambda \nabla_{\theta} g(\theta_{k})$$

$$\mathsf{Adam\ optimizer,\ fixed\ learning\ rate}$$

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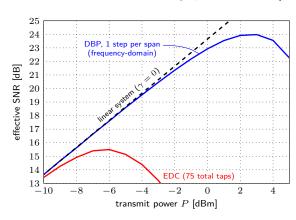


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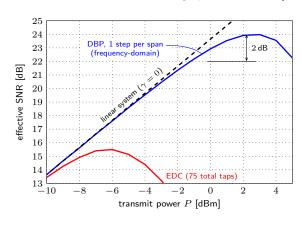
$$\mathsf{Adam optimizer, fixed learning rate}$$

Iteratively prune (set to 0) outermost filter taps during gradient descent



Parameters similar to [Ip and Kahn, 2008]:

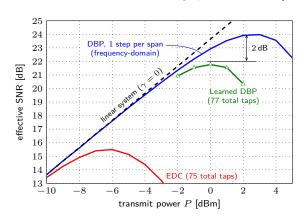
- $25 \times 80 \, \mathrm{km} \, \mathrm{SSFM}$
- Gaussian modulation
- RRC pulses (0.1 roll-off)
- 10.7 Gbaud
- 2 samples/symbol processing
- single channel, single pol.



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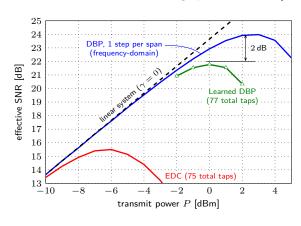
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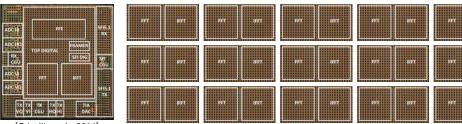
- $\gg 1000$ total taps (70 taps/step) $\implies > 100 \times$ complexity of EDC
- Learned approach uses only 77 total taps: alternate 5 and 3 taps/step and use different filter coefficients in all steps [Häger and Pfister, 2018a]



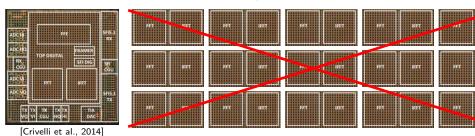
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- Can outperform "ideal DBP" in the nonlinear regime [Häger and Pfister, 2018b]



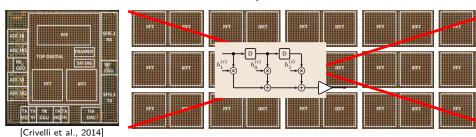
[Crivelli et al., 2014]



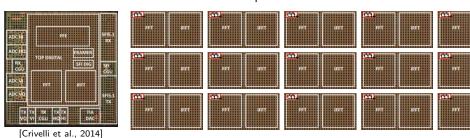
[[]Fougstedt et al., 2017], Time-domain digital back propagation: Algorithm and finite-precision implementation aspects, (OFC)

[[]Fougstedt et al., 2018], ASIC implementation of time-domain digital back propagation for coherent receivers, (PTL)

Sherborne et al., 2018, On the impact of fixed point hardware for optical fiber nonlinearity compensation algorithms, (JLT)



• Our linear steps are very short symmetric FIR filters (as few as 3 taps)



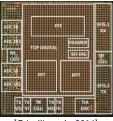
- Our linear steps are very short symmetric FIR filters (as few as 3 taps)
- 28-nm ASIC at 416.7 MHz clock speed (40 GHz signal)
 - Only 5-6 bit filter coefficients via learned quantization
 - Hardware-friendly nonlinear steps (Taylor expansion)
 - All FIR filters are fully reconfigurable

[[]Fougstedt et al., 2018], ASIC implementation of time-domain digital backpropagation with deep-learned chromatic dispersion filters, (ECOC)



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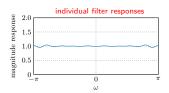
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- $< 2 \times$ power compared to EDC [Crivelli et al., 2014, Pillai et al., 2014]

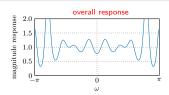
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Why Does The Learning Approach Work?

Previous work: design a single filter or filter pair and use it repeatedly.

⇒ Good overall response only possible with very long filters.





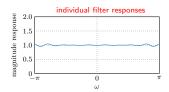
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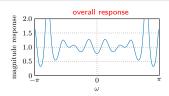
- "We also note that [...] 70 taps, is much larger than expected"
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- "Since backpropagation requires multiple iterations of the linear filter, amplitude distortion due to ringing accumulates (Goldfarb & Li, 2009)"

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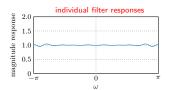
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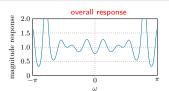
The learning approach uncovered that there is no such requirement! [Lian, Häger, Pfister, 2018], What can machine learning teach us about communications? (ITW)

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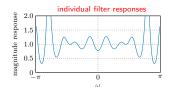
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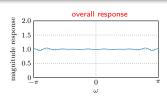




Sacrifice individual filter accuracy, but different response per step.

⇒ Good overall response even with very short filters by joint optimization.



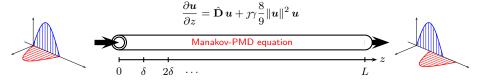


CHALMERS

Outline

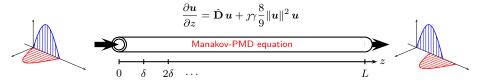
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- Conclusions

Evolution of Polarization-Multiplexed Signals

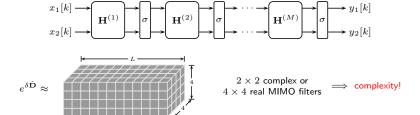


- Jones vector $\boldsymbol{u} \triangleq (u_1(t,z), u_2(t,z))^{\top}$ with complex baseband signals
- linear operator $\hat{\mathbf{D}}$: attentuation, chromatic & polarization mode dispersion

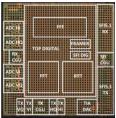
Evolution of Polarization-Multiplexed Signals

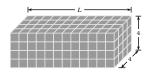


- Jones vector $\boldsymbol{u} \triangleq (u_1(t,z), u_2(t,z))^{\top}$ with complex baseband signals
- linear operator $\hat{\mathbf{D}}$: attentuation, chromatic & polarization mode dispersion
- Split-step method: alternate linear and nonlinear steps $\sigma(x) = xe^{j\gamma \frac{8}{9}\delta\|x\|^2}$



Real-Time Compensation of Polarization Impairments

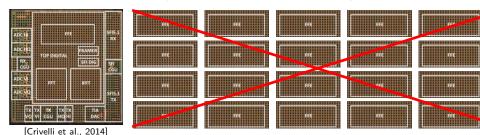




[Crivelli et al., 2014]

- time-varying effects (e.g., drifts) & apriori unknown realizations
- adaptive filtering (via stochastic gradient descent) required

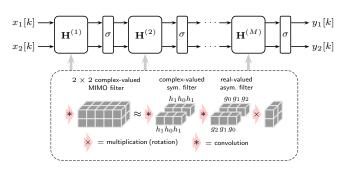
Real-Time Compensation of Polarization Impairments



- time-varying effects (e.g., drifts) & apriori unknown realizations
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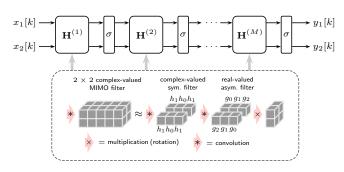
Using (and updating) full MIMO filters in each step is not feasible.

Our approach: Factorize each MIMO Filter



- 5-tap real-valued filters to approximate first-order PMD (DGD)
- Memoryless rotations $\binom{a-b^*}{b-a^*}$, where $a,b\in\mathbb{C}$ (4 real parameters)

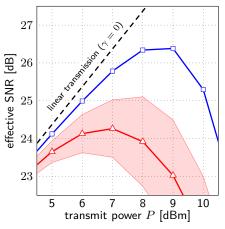
Our approach: Factorize each MIMO Filter



- 5-tap real-valued filters to approximate first-order PMD (DGD)
- Memoryless rotations $\binom{a-b^*}{b-a^*}$, where $a,b\in\mathbb{C}$ (4 real parameters)
- Assumes no knowledge about PMD realizations or accumulated PMD
- FIR-filter based! Avoids frequency-domain (FFT-based) filtering

[Goroshko et al., 2016], Overcoming performance limitations of digital back propagation due to polarization mode dispersion, (CTON) [Czegledi et al., 2017], Digital backpropagation accounting for polarization-mode dispersion, (Opt. Express) [Liga et al., 2018], A PMD-adaptive DBP receiver based on SNR optimization, (OFC)

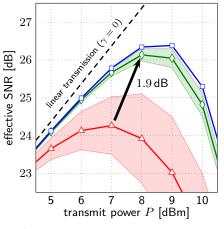
Results (32 Gbaud, 10×100 km, 0.2 ps/ $\sqrt{\text{km}}$ PMD)



-D- LDBP (4 StPS), no PMD → PMD comp. after LDBP

Similar parameters & simulation setup compared to [Czegledi et al., 2016], results averaged over 40 PMD realizations

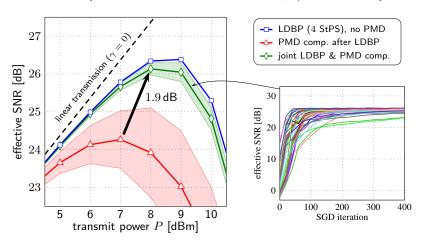
Results (32 Gbaud, 10×100 km, 0.2 ps/ $\sqrt{\text{km}}$ PMD)



-□- LDBP (4 StPS), no PMD
-□- PMD comp. after LDBP
-□- joint LDBP & PMD comp.

ullet Similar parameters & simulation setup compared to [Czegledi et al., 2016], results averaged over 40 PMD realizations

Results (32 Gbaud, 10×100 km, 0.2 ps/ $\sqrt{\text{km}}$ PMD)



- Similar parameters & simulation setup compared to [Czegledi et al., 2016], results averaged over 40 PMD realizations
- Reliable convergence "from scratch" + only 9 real parameters per step

Related and Recent Works

Learned digital backpropagation

- [Häger & Pfister, 2018], Nonlinear Interference Mitigation via Deep Neural Networks, (OFC)
- [Häger & Pfister, 2018], Deep Learning of the Nonlinear Schrödinger Equation in Fiber-Optic Communications, (ISIT)
- [Lian, Häger, Pfister, 2018], What can machine learning teach us about communications? (ITW)
- [Häger et al., 2019], Revisiting multi-step nonlinearity compensation with machine learning (ECOC)

Wideband & WDM signals (alternating filter banks and nonlinearities)

• [Häger and Pfister, 2018], Wideband time-domain digital backpropagation via subband processing and deep learning, (ECOC)

ASIC implementation & finite-precision aspects

 [Fougstedt et al., 2018], ASIC implementation of time-domain digital backpropagation with deep-learned chromatic dispersion filters, (ECOC)

Experimental demonstrations & implementation aspects (e.g., phase noise)

- [Sillekens et al., 2020], Experimental demonstration of learned time-domain digital back-propagation, (arXiv)
- [Bitachon et al., 2020]. Deep learning based digital back propagation with polarization state rotation & phase noise invariance, (OFC)

The Bigger Picture

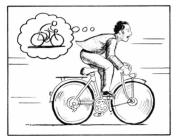
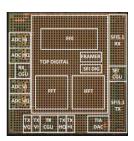


Figure 1. A World Model, from Scott McCloud's Understanding Comics. (McCloud, 1993; E, 2012)



[Crivelli et al., 2014]

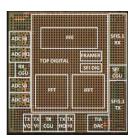
• Optical receivers build models of their "environment"

Ha and Schmidhuber, 2018, "World Models", arXiv:1803.10122 [cs.LG]

The Bigger Picture



Figure 1. A World Model, from Scott McCloud's Understanding Comics. (McCloud, 1993; E, 2012)



[Crivelli et al., 2014]

- Optical receivers build models of their "environment"
- Currently these models are linear and/or rigid (non-adaptive)
- Interpretable physics-based "multi-layer" models for machine learning can be obtained by exploiting our existing domain knowledge

Ha and Schmidhuber, 2018, "World Models", arXiv:1803.10122 [cs.LG]

neural-network-based ML

universal function approximators

good designs require experience and fine-tuning

> black boxes, difficult to "open"

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Conclusions

neural-network-based ML	model-based ML
universal function approximators	application-tailored
good designs require experience and fine-tuning	relies on domain knowledge (algorithms, physics,)
black boxes, difficult to "open"	familiar building blocks (e.g., FIR filters) can enable interpretability

neural-network-based MI model-based ML universal function approximators application-tailored relies on domain knowledge good designs require (algorithms, physics, ...) experience and fine-tuning black boxes. familiar building blocks (e.g., FIR difficult to "open" filters) can enable interpretability

Thank you!







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