# Agenda

- Introduction of discussion leader Marco Secondini
- Errata
- Presentation by Christian Häger (30 min)
- Discussion ( $\approx$  60 min)
- Questions and comments from the audience
- Final decision by examiner

# On Signal Constellations and Coding for Long-Haul Fiber-Optical Systems

#### Christian Häger

 $\label{eq:charge} \mbox{ Department of Signals and Systems, Chalmers University of Technology, Gothenburg, Sweden, $$christian.haeger@chalmers.se$$ 



FIBER-OPTIC COMMUNICATIONS
RESEARCH CENTER

Licentiate Seminar, May 9, 2014



 Higher-order signal constellations/modulation formats for optical communication to increase spectral efficiency

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#### Outline

1. Fiber-optical channel modeling

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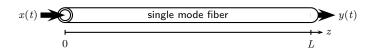
- 1. Fiber-optical channel modeling
- 2. Constellation design in the presence of severe nonlinear phase noise
- 3. Low-complexity detection for polarization-multiplexed (PM) signals

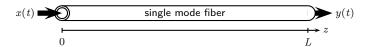
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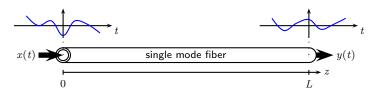
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- 4. Bit mapper optimization for protograph codes

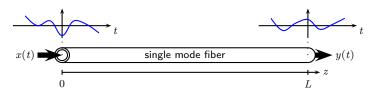




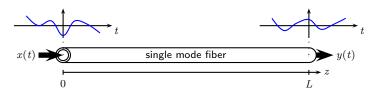
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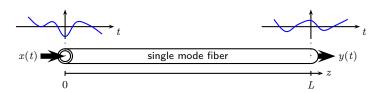


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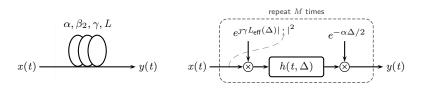


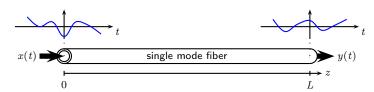
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$$x(t) \xrightarrow{\alpha, \beta_2, \gamma, L} y(t)$$



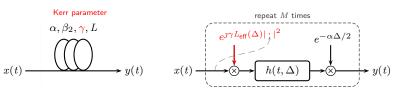
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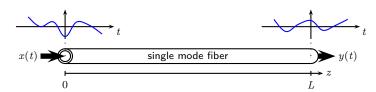


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Channel Modeling

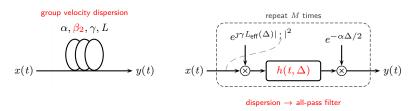


nonlinear Kerr effect → phase rotation

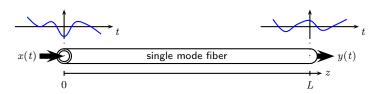


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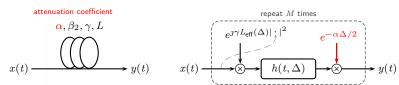


# Fiber-Optical Channel Modeling



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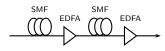


attenuation → decaying signal power

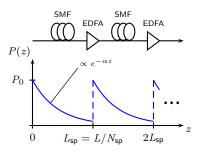
# Optical Amplification and Noise

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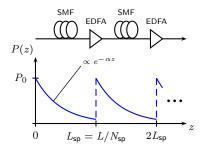
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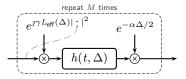


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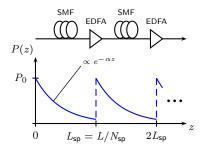


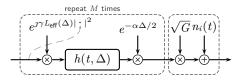
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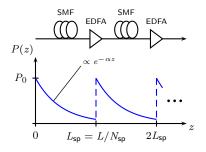


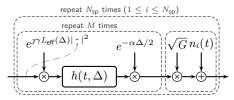
### Optical Amplification and Noise



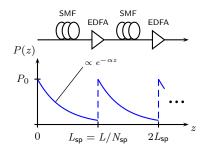


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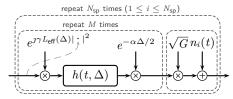




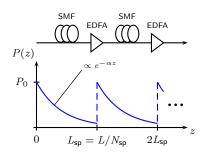
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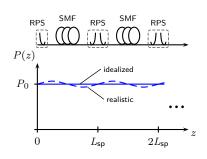


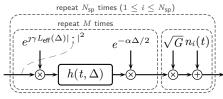




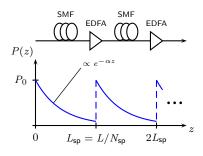
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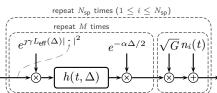


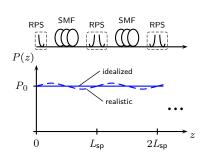


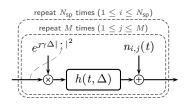


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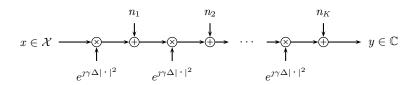




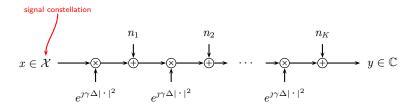


• Assume  $\beta_2 = 0$  (zero-dispersion fiber)

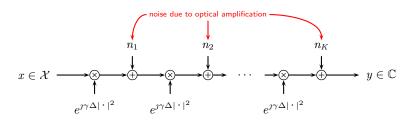
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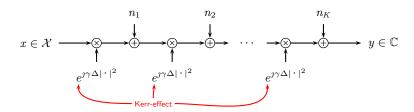
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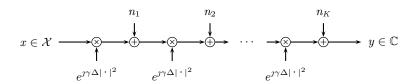
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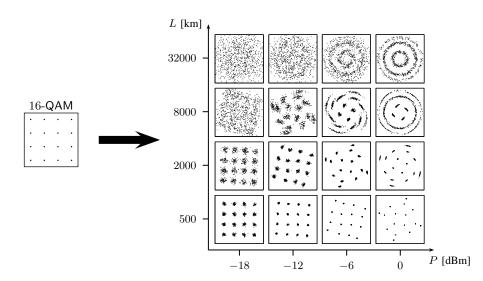


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- Extensive work on this model, e.g., [Mecozzi, 1994],
   [Turitsyn et al., 2003], [Ho, 2005], [Yousefi and Kschischang, 2011]

### 16-QAM

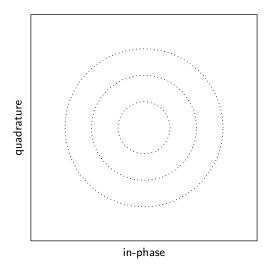


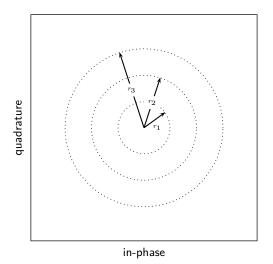


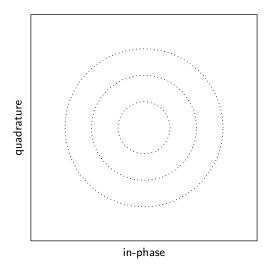


quadrature

in-phase

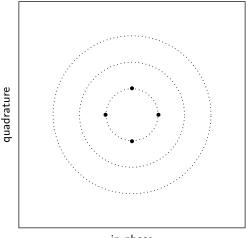




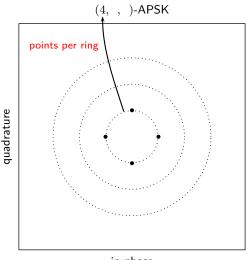


### $\label{eq:amplitude_phase-Shift Keying (APSK), Example} Amplitude \ Phase-Shift \ Keying \ (APSK), \ Example$

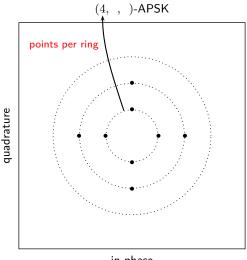
 $( \ , \ , \ )$ -APSK



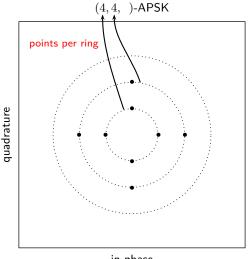
in-phase



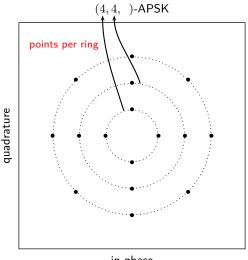
in-phase



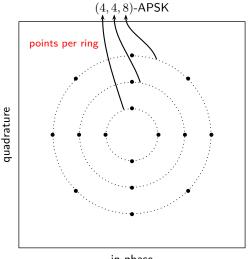
in-phase



in-phase

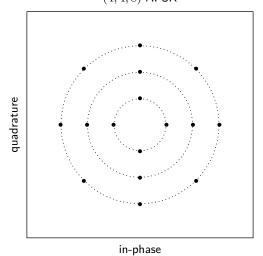


in-phase

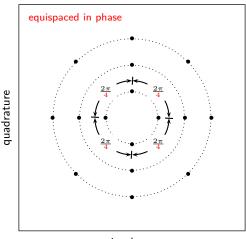


in-phase

# Amplitude Phase-Shift Keying (APSK), Example (4,4,8)-APSK

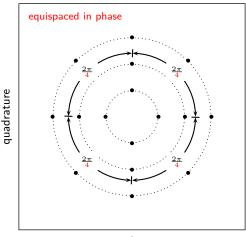


(4, 4, 8)-APSK



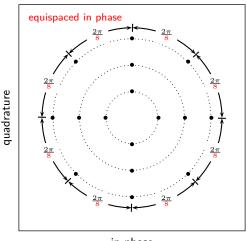
in-phase

(4, 4, 8)-APSK



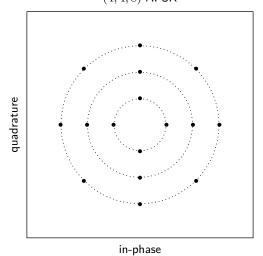
in-phase

(4, 4, 8)-APSK

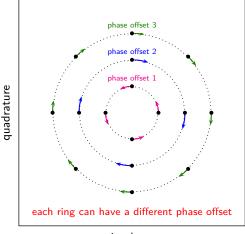


in-phase

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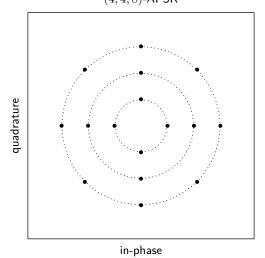


 $(4,4,8)\text{-}\mathsf{APSK}$ 



in-phase

# Amplitude Phase-Shift Keying (APSK), Example (4,4,8)-APSK



quadrature

in-phase

quadrature another example

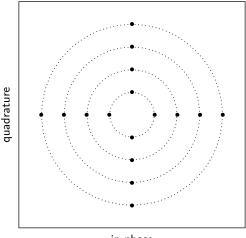
in-phase

(4, 4, 4, 4)-APSK

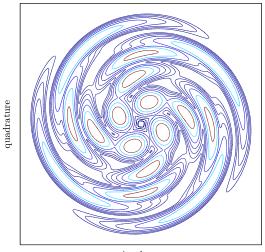
quadrature

in-phase

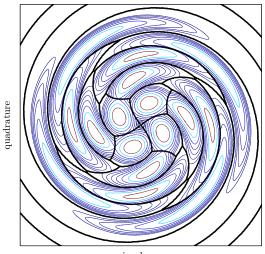
(4, 4, 4, 4)-APSK



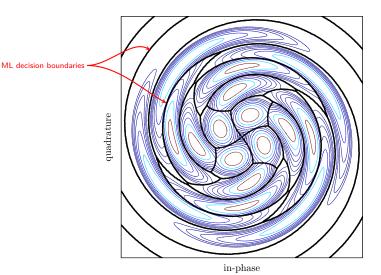
in-phase

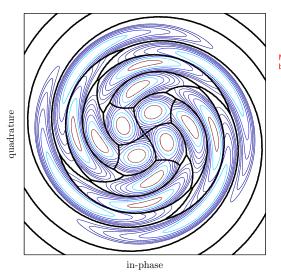


in-phase



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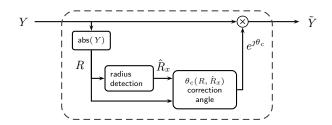




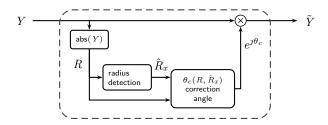
ML detection possible, but not practical.

#### Nonlinear Phase Postcompensation

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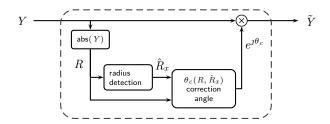


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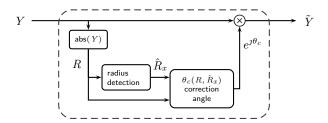
• Building block for suboptimal (but practical) two-stage detector

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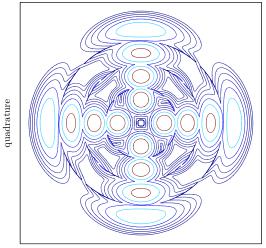


- Building block for suboptimal (but practical) two-stage detector
- ullet Characterization of the PDF of  $ilde{Y}$

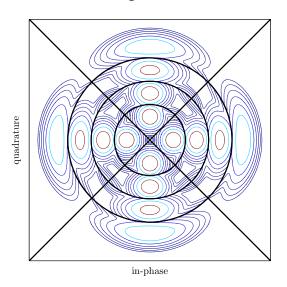
#### Nonlinear Phase Postcompensation

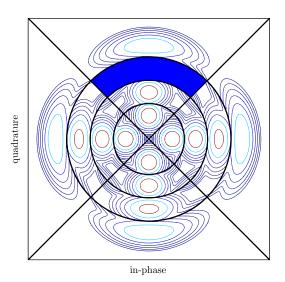


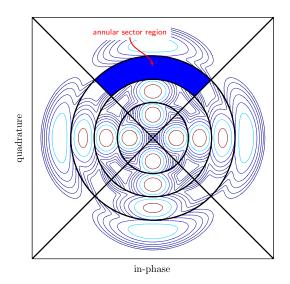
- Building block for suboptimal (but practical) two-stage detector
- Characterization of the PDF of  $\tilde{Y}$
- Necessary to compute, e.g., bit error probability



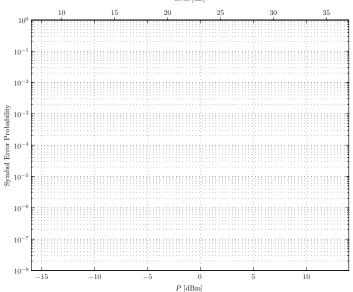
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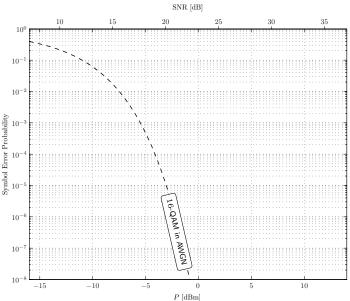


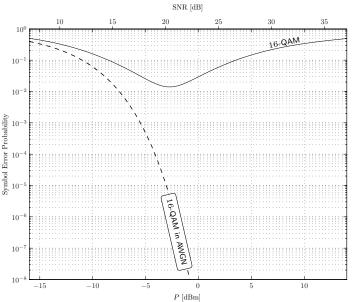


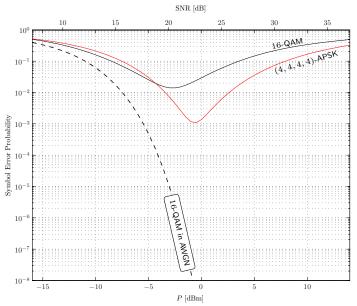


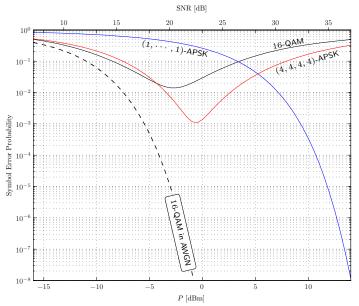


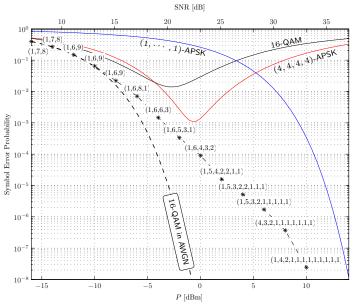










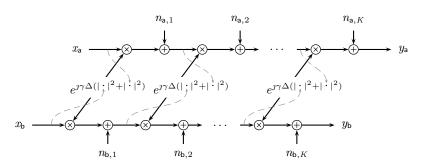


• Extension of the previous channel model to polarization multiplexed signals

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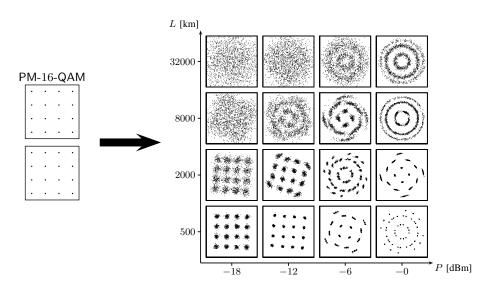


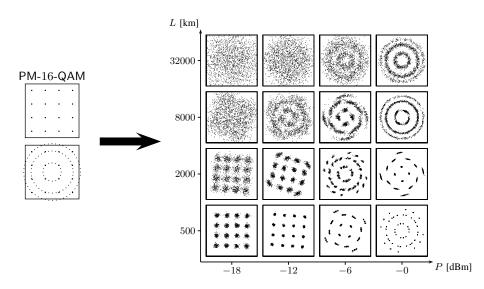
#### PM-16-QAM

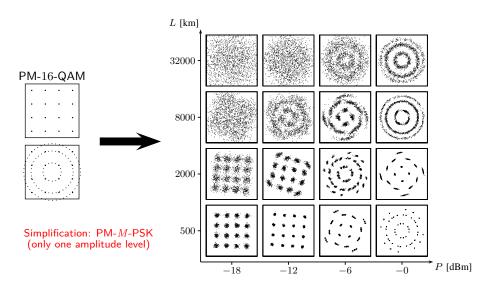




# 







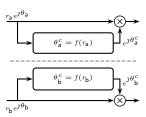
#### Scatterplot for pol. a



Scatterplot for pol. a



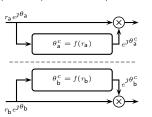
#### separate compensation in each polarization



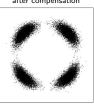
Scatterplot for pol. a



separate compensation in each polarization



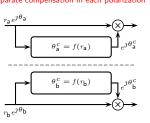
after compensation



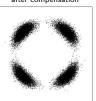
Scatterplot for pol. a



separate compensation in each polarization



after compensation



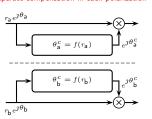
Scatterplot for pol. a



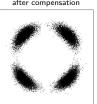
#### Scatterplot for pol. a



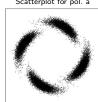
#### separate compensation in each polarization



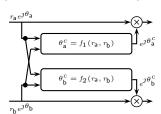
after compensation



Scatterplot for pol. a



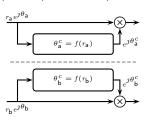
#### compensation based on both received amplitudes



#### Scatterplot for pol. a



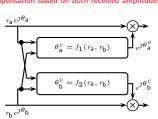
#### separate compensation in each polarization



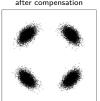




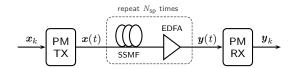
compensation based on both received amplitudes

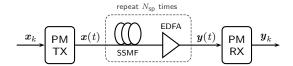


after compensation

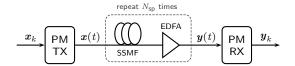


less phase noise → better SER

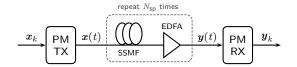




• Dispersive fibers,  $\beta_2 \neq 0$ 

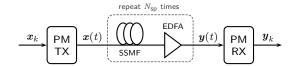


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#### Channel Model for PM Transmission including Dispersion



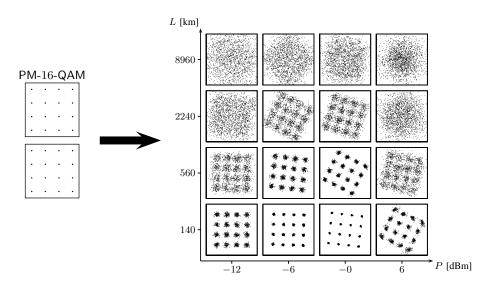
- Dispersive fibers,  $\beta_2 \neq 0$
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- No exact characterization of the statistical relationship between transmitted symbols  $x_k = (x_{a,k}, x_{b,k})$  and received samples  $y_k = (y_{a,k}, y_{b,k})$
- Under some assumptions, several works give theoretical justification for a Gaussian noise (GN) model, e.g., [Beygi et al., 2012], [Carena et al., 2012]

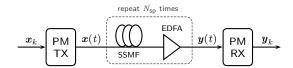
#### PM-16-QAM

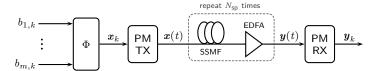


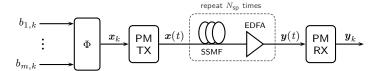


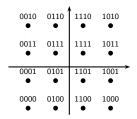
# 



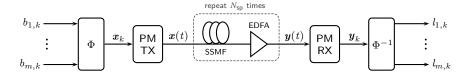


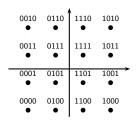




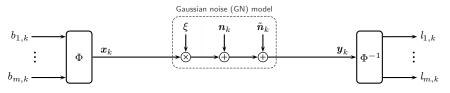


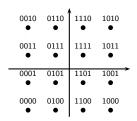
(in both polarizations)



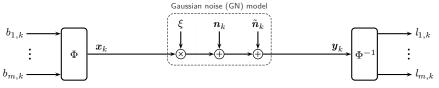


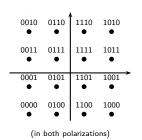
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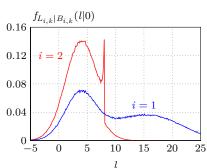


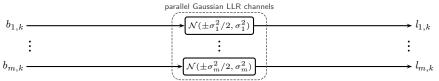


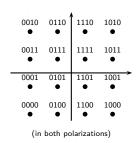
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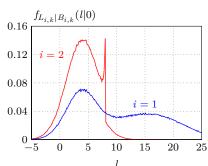


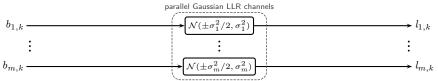


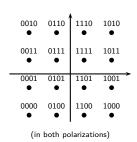


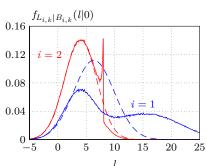


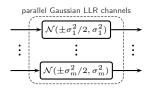




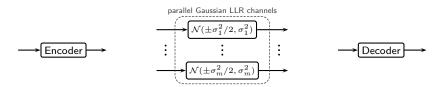




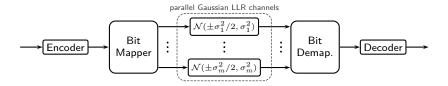




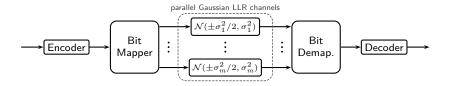
• Approximate setup: parallel Gaussian LLR channels with different qualities (constellation size determines the number of channels)



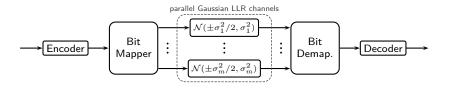
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- Fix one binary FEC encoder/decoder pair



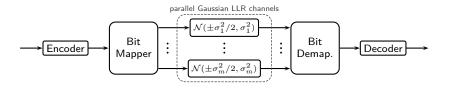
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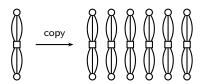
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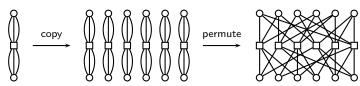


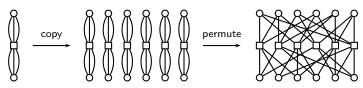
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codeword = 
$$(c_1, c_2, c_3, c_4, c_5, c_6, ...)$$

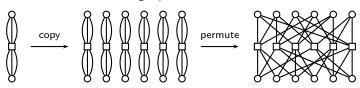




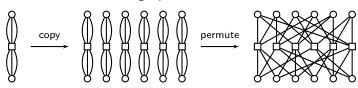




- Main idea: obtain Tanner graph from a small protograph via copy-and-permute procedure
- Allows for high-speed hardware implementation

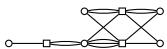


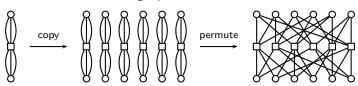
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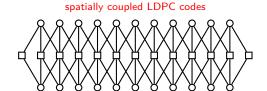
#### AR4 IA codes

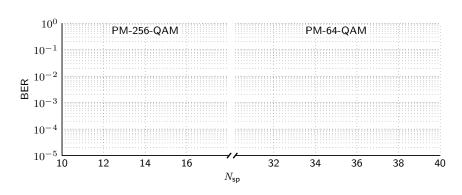


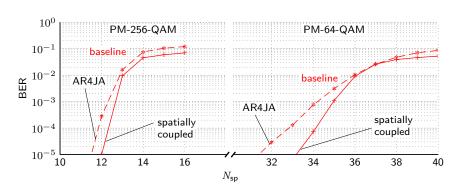


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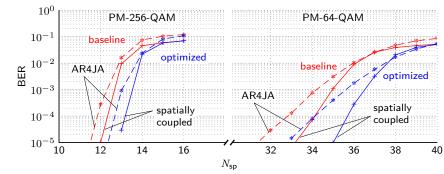
# AR4JA codes

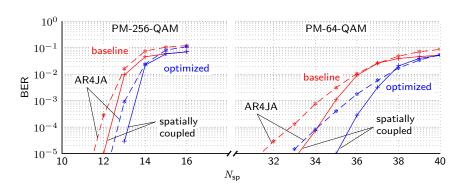




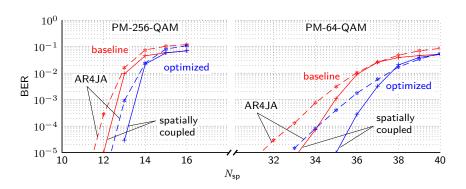




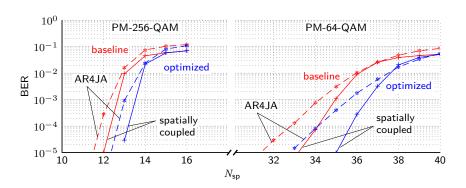




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# Thank you!



#### References



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